

## Appendix B

# Example Calculation – Case Study building: Dunedin URM typology 2





## **Structural Calculation Set**

# Example calculations for a case study building in Dunedin, a single storey unreinforced masonry, commercial office building

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## Calculation

#### Input parameters

Building height H = 3 m

Importance Level IL2

Lateral Load Resisting System Unreinforced masonry walls

Period of vibration  $T_1 = 0.4 s$  Using EAG, Clause B

Structural ductility  $\mu = 1.25$ 

Soil class as per NZS1170.5 C NZS 1170.5 CI 3.1.3

Shear wave velocity  $V_{s30} = 400 \, m/s$  This study looked at a range of

Vs30 including most common NZ's site class IV with Vs30 of

275 m/s.

$$T_{\rm eff} = 2\pi \sqrt{\frac{m_{\rm eff}}{g.k_{\rm eff}}}$$

Effective Period SDOF [EAG, C2.13]

#### 1. Structural Demand

Spectral shape factor

#### Class C shallow soil

The values for the MRS and NITH methods are given by:

$$C_{\rm h}(0) = 1.33$$

For 
$$0 < T < 0.1$$

$$C_h(T) = 1.33 + 1.60 (T/0.1)$$

For 0.1 < T < 0.3

$$C_{\rm h}(T) = 2.93$$

For 
$$0.3 \le T \le 1.5$$

$$C_{\rm h}(T) = 2.0 (0.5/T)^{0.75}$$

For  $1.5 < T \le 3$ 

$$C_{\rm h}(T) = 1.32/T$$

For 3 < T

$$C_{\rm h}(T) = 3.96/T^2$$

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Spectral shape factor

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$$C_h(T) = 2.36$$

$$C_h(0) = 1.33$$

$$Z = 0.13$$

$$R = 1.0$$

Calculated return period factor hazard

$$ZR_{calculated} = 0.13$$

Maximum hazard return period

$$ZR_{max} = 0.7$$

$$ZR = min(ZR_{calculated}, ZR_{max})$$

$$ZR = min(0.13, 0.7)$$

$$ZR = 0.13$$

Maximum near fault factor

$$N_{max}(T) = 1.0$$

Unity for periods less than 1.5 s

Near fault factor

$$N(T,D) = 1.0$$

C(T) = 0.31 g

Equivalent to maximum near fault factor for Wellington CBD.

Elastic site hazard spectrum

$$C(T) = C_h(T) \cdot ZR \cdot N(T, D)$$

$$C(T) = 2.36 \cdot 0.13 \cdot 1.0$$

**Ductility factor** 

$$k_{\mu} = (\mu - 1) \cdot \frac{T_1}{0.7} + 1$$

$$k_{\mu} = (1.25 - 1) \cdot \frac{0.4}{0.7} + 1$$

$$k_{\mu}=1.14$$

$$k_{"} = 1.0$$

The ductility factor shall be set to

1.0 for ADRS spectra.

Structural performance factor

$$S_p = max(0.7, 1.3 - 0.3 \cdot \mu)$$

$$S_p = max(0.7, 1.3 - 0.3 \cdot 1.25)$$

$$S_p = 0.925$$

Horizontal design action coefficient

$$C_d(T) = max \left( 0.03 \cdot R_u, \left( \frac{Z}{20} + 0.02 \right) \cdot R_u, C(T) \cdot S_p / k_\mu \right)$$

$$C_d(T) = max\left(0.03 \cdot 1.0, \left(\frac{0.13}{20} + 0.02\right) \cdot 1.0, 0.31 \cdot 0.925/1.0\right)$$

$$C_d(T) = 0.284 g$$



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Spectral acceleration capacity

$$S_a = C_d(T)$$
  
$$S_a = 0.284 g$$

[EAG, C3.5]

Spectral displacement capacity

$$S_d = 9.81 \cdot \frac{T^2}{4 \cdot \pi^2} \cdot S_a$$
$$S_d = 9.81 \cdot \frac{0.4^2}{4 \cdot \pi^2} \cdot 0.284$$

[NZS1170.5]

$$S_d = 0.0131 m$$

Hysteretic damping

$$\xi_{hy} = 2\%$$

[EAG, Tab C2D1]

The hysteretic damping for the structure is based on Table C2D.1 of the EQ Assess Guidelines and snipped below.

Inherent damping

$$\xi_0 = 5\%$$

EAG Section C2D.3.2

System damping

$$\xi_{sys} = \xi_0 + \xi_{sys}$$
  
$$\xi_{sys} = 5\% + 2\%$$
  
$$\xi_{sys} = 7\%$$

Spectral damping reduction factor

$$k_{\xi} = \left(\frac{7}{2 + \xi_{sys}}\right)^{0.5}$$
$$k_{\xi} = \left(\frac{7}{2 + 7}\right)^{0.5}$$
$$k_{\xi} = 0.88$$

In special cases of rocking URM buildings, Table C2D.1does not apply. It is not known whether rocking will govern for the URM structures in this study, so it is assumed that they will exhibit some hysteretic damping in line with Table C2D.1 which will lead to a smaller assumed structural backbone in this study.

Inelastic spectral acceleration

$$S_{a,inelastic} = S_a \cdot k_{\xi}$$
  
 $S_{a,inelastic} = 0.284 \cdot 0.88$   
 $S_{a,inelastic} = 0.251$ 

Inelastic spectral displacement

$$\begin{split} S_{d,inelastic} &= \frac{9.81 \cdot T^2 \cdot S_{a,inelastic}}{4 \cdot \pi^2} \\ S_{a,inelastic} &= \frac{9.81 \cdot 0.4^2 \cdot 0.251}{4 \cdot \pi^2} \\ S_{a,inelastic} &= 0.0100 \ m \end{split}$$

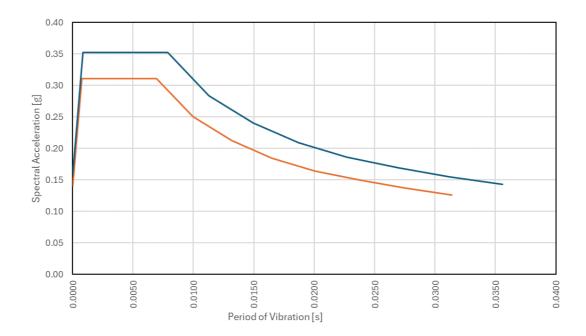
Repeating this process for different period yields the inelastic NZS1170.5:2004 demand curve.

Table \*: Demand curve parameters

T	$C_h$	С	$C_d$	$S_d$ for $C_d$	$S_{a,inelastic}$	$\mathcal{S}_{d,inelastic}$
0	1.33	0.17	0.16	0.0000	0.14	0.0000
0.1	2.93	0.38	0.35	0.0009	0.31	0.0008
0.2	2.93	0.38	0.35	0.0035	0.31	0.0031

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0.3	2.93	0.38	0.35	0.0079	0.31	0.0069			
0.4	2.36	0.31	0.28	0.0113	0.25*	0.0100*			
0.5	2	0.26	0.24	0.0149	0.21	0.0132			
0.6	1.74	0.23	0.21	0.0187	0.18	0.0165			
0.7	1.55	0.20	0.19	0.0227	0.16	0.0200			
8.0	1.41	0.18	0.17	0.0270	0.15	0.0238			
0.9	1.29	0.17	0.16	0.0312	0.14	0.0275			
1	1.19	0.15	0.14	0.0356	0.13	0.0314			
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<sup>\*</sup>Values match the hand calculation



#### 2. Structural Equivalent Capacity

In this step, a backbone that equates to the buildings governing score is sought. What is known initially is that the building is on the earthquake-prone register, therefore this governing element must have scored approximately 20%NBS (plus or minus 10%). We also know that if we had the backbone of the structure and plotted it on an ADRS, it would score around 20%NBS.

From this information, and knowing key characteristics of the building (e.g. its stiffness and ductility), we can work backwards from the ADRS curve to generate an approximate backbone for the element of the structure that governs the %NBS score.

Site elastic spectrum at period of zero

$$C(0) = C_h(0) \cdot ZR_{final} \cdot N(T, D)$$

$$C(0) = 1.33 \cdot 0.13 \cdot 1.0$$

$$C(0) = 0.173$$
[NZS1170.5, Eq.3.1(1)]

Horizontal design action coefficient

$$\begin{split} C_d(0) &= max \left( 0.03 \cdot R, \left( \frac{Z}{20} + 0.02 \right) \cdot R, C(0) \cdot S_p / k_\mu \right) \\ C_d(0) &= max \left( 0.03 \cdot 1.0, \left( \frac{0.13}{20} + 0.02 \right) \cdot 1.0, 1.33 \cdot 0.925 / 1.0 \right) \\ C_d(0) &= 0.16 \end{split}$$

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Ratio between PGA to spectral acceleration

$$R_{PGA/SA} = \frac{C_d}{C_d(0)}$$
 $R_{PGA/SA} = \frac{0.284}{0.16}$ 
 $R_{PGA/SA} = 0.563$ 

Ultimate spectral displacement

$$\begin{split} S_{du,inelastic} &= S_{d,inelastic} \cdot \mu \\ S_{du,inelastic} &= 0.0100 \cdot 0.125 \\ S_{du,inelastic} &= 0.0125 \end{split}$$

Secant period of the structure

$$T_s = \sqrt{\frac{4 \cdot \pi^2 \cdot S_{du}}{9.81 \cdot S_{a,inelastic}}}$$

$$T_s = \sqrt{\frac{4 \cdot \pi^2 \cdot 0.0125}{9.81 \cdot 0.251}}$$

$$T_s = 0.45 s$$

The intersection of the secant period line and the inelastic demand spectrum represents the ultimate displacement of a building rated 100%NBS.

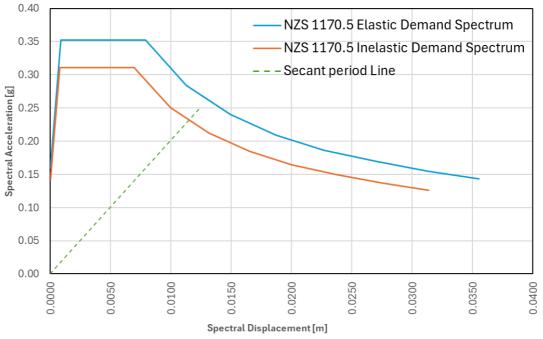


Figure: Inelastic demand curve against fictious backbone of equal stiffness and ductility to chosen structure.

Spectral acceleration of 100%NBS structure

$$S_{a,100} = 0.232$$

By interpolation

Spectral displacement of 100%NBS structure

$$S_{du,100} = 9.81 \cdot S_{a,100} \cdot \frac{T_s^2}{4\pi^2}$$

$$S_{du,100} = 9.81 \cdot 0.232 \cdot \frac{0.4^2}{4\pi^2}$$

$$S_{du,100} = 0.0115 m$$

To establish the equivalent backbone of the earthquake-prone structure, the 100%NBS backbone is scaled down to the given %NBS.

Spectral acceleration at NBS  $S_{c}$ 

$$S_{a,nbs} = \%NBS \cdot S_{a,100}$$
  
 $S_{d,nbs} = 20\% \cdot 0.232$   
 $S_{d,nbs} = 0.046 g$ 

Spectral displacement at NBS

$$S_{du,nbs} = \%NBS \cdot S_{d,100}$$
  
 $S_{du,nbs} = 20\% \cdot 0.0115$   
 $S_{du,nbs} = 0.0023 m$ 

Yield spectral displacement at NBS

$$S_{dy,nbs} = \frac{S_{du}}{\mu}$$
 
$$S_{dy,nbs} = \frac{0.0023}{1.25}$$
 
$$S_{dy,nbs} = 0.0018 m$$

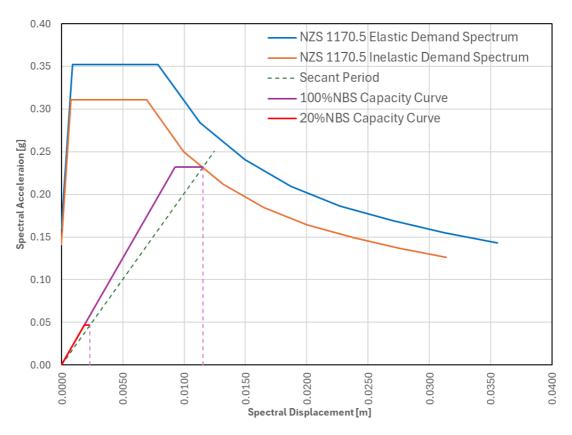


Figure: Inelastic demand curve (orange) against backbone of equal stiffness and ductility for case study building

As a back check, the %NBS can be yielded by the ratio of the ultimate displacement for the 100%NBS curve and the final %NBS curve.

%NBS of the structure

$$\%NBS = \frac{S_{d,nbs}}{S_{d,100}}$$
$$\%NBS = \frac{0.0023}{0.0115}$$
$$\%NBS = 20\%$$



Plot the point ( $\Delta_{\text{prob},20\%}$ , Sa $_{20\%}$ ) over the inelastic ADRS curve. Determine the Duls demand by extending a line radiating out from the origin of this point through the point ( $\Delta \text{prob}_{20\%}$ , Sa $_{20\%}$ ) to intersect with the ADRS curve. The %NBS earthquake score for the SDOF is the ratio of  $\Delta_{\text{ULS}}$  and  $\Delta \text{prob}_{20\%}$ 

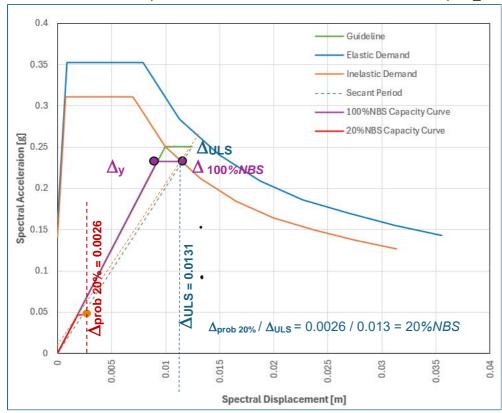


Figure: 20%NBS (no upgrade) backbone curve

#### 3. Adjustment of Backbone for Inherent Capacity

As described in supporting documents, the backbone generated for the structure is increased by an inherent capacity factor of 2.0.

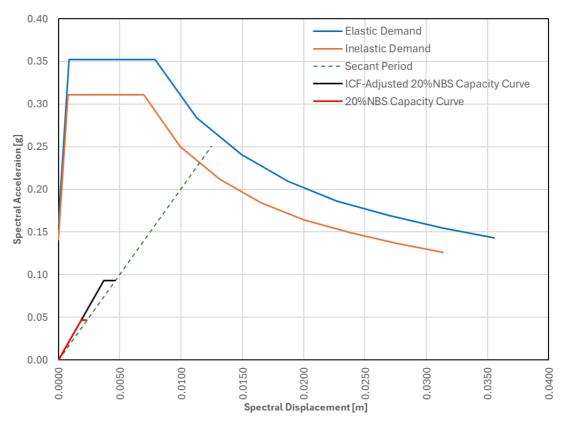


Figure: Increase in structural capacity backbone by the chosen inherent capacity factor.

Ultimate spectral displacement including inherent capacity factor

$$S_{du,ICF} = ICF \cdot S_{du,nbs}$$

 $S_{du,ICF} = 2.0 \cdot 0.0023$ 

 $S_{du,ICF}=0.0046\ m$ 

Yield spectral displacement including inherent capacity factor

$$S_{dy,ICF} = ICF \cdot S_{dy,nbs}$$

 $S_{dy,ICF} = 2.0 \cdot 0.0018$ 

 $S_{dy,ICF} = 0.0037 m$ 

Spectral acceleration

$$S_{a,ICF} = ICF \cdot S_{a,nbs}$$

 $S_{a,ICF} = 2.0 \cdot 0.046$ 

 $S_{a,ICF} = 0.093 g$ 

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#### **Calculation Sheet**

### 4. Displacement Limits associated with Damage States

HAZUS relates defined damage states for different structural typologies and code levels to specific displacement limits.

Build	<b>Building Properties</b>			tory Drift at	Threshold of	Damage	Spectral Displacement (Inches)							
Tuna	Height (	(Inches)		Ś	tate	ŭ	Sligi	ht	Mode	rate	Exten	sive	Comp	lete
Туре	Roof	Modal	Slight	Moderate	Extensive	Complete	Median	Beta	Median	Beta	Median	Beta	Median	Beta
S4M	720	540	0.0021	0.0034	0.0086	0.0233	1.15	0.81	1.85	0.79	4.62	0.94	12.60	1.00
S4H	1,872	1,123	0.0016	0.0026	0.0064	0.0175	1.80	0.73	2.88	0.76	7.21	0.90	19.66	0.96
S5L	288	216	0.0024	0.0048	0.0120	0.0280	0.52	1.20	1.04	1.11	2.59	1.08	6.05	0.95
S5M	720	540	0.0016	0.0032	0.0080	0.0187	0.86	0.85	1.73	0.83	4.32	0.94	10.08	0.99
S5H	1,872	1,123	0.0012	0.0024	0.0060	0.0140	1.35	0.72	2.70	0.75	6.74	0.92	15.72	0.96
C1L	240	180	0.0040	0.0064	0.0160	0.0400	0.72	0.98	1.15	0.94	2.88	0.90	7.20	0.96
C1M	600	450	0.0027	0.0043	0.0107	0.0267	1.20	0.73	1.92	0.77	4.80	0.84	12.00	0.98
C1H	1,440	864	0.0020	0.0032	0.0080	0.0200	1.73	0.71	2.76	0.80	6.91	0.94	17.28	1.01
C2L	240	180	0.0032	0.0061	0.0158	0.0400	0.58	1.12	1.10	1.08	2.84	1.06	7.20	0.93
C2M	600	450	0.0021	0.0041	0.0105	0.0267	0.96	0.86	1.83	0.83	4.74	0.80	12.00	0.98
C2H	1,440	864	0.0016	0.0031	0.0079	0.0200	1.38	0.73	2.64	0.75	6.82	0.92	17.28	0.97
C3L	240	180	0.0024	0.0048	0.0120	0.0280	0.43	1.19	0.86	1.15	2.16	1.16	5.04	0.92
СЗМ	600	450	0.0016	0.0032	0.0080	0.0187	0.72	0.90	1.44	0.86	3.60	0.90	8.40	0.96
СЗН	1,440	864	0.0012	0.0024	0.0060	0.0140	1.04	0.73	2.07	0.74	5.18	0.90	12.10	0.95
PC1	180	135	0.0032	0.0051	0.0128	0.0350	0.43	1.14	0.69	1.14	1.73	1.17	4.73	0.99
PC2L	240	180	0.0032	0.0051	0.0128	0.0350	0.58	1.14	0.92	1.10	2.31	1.10	6.30	0.93
PC2M	600	450	0.0021	0.0034	0.0086	0.0233	0.96	0.87	1.54	0.83	3.85	0.92	10.50	1.00
PC2H	1,440	864	0.0016	0.0026	0.0064	0.0175	1.38	0.74	2.21	0.76	5.55	0.91	15.12	0.96
RM1L	240	180	0.0032	0.0051	0.0128	0.0350	0.58	1.20	0.92	1.17	2.31	1.17	6.30	0.94
RM1M	600	450	0.0021	0.0034	0.0086	0.0233	0.96	0.92	1.54	0.89	3.85	0.88	10.50	0.96
RM2L	240	180	0.0032	0.0051	0.0128	0.0350	0.58	1.14	0.92	1.10	2.31	1.15	6.30	0.92
RM2M	600	450	0.0021	0.0034	0.0086	0.0233	0.96	0.90	1.54	0.87	3.85	0.86	10.50	0.96
RM2H	1,440	864	0.0016	0.0026	0.0064	0.0175	1.38	0.75	2.21	0.75	5.55	0.85	15.12	0.94
URML	180	135	0.0024	0.0048	0.0120	0.0280	0.32	1.15	0.65	1.19	1.62	1.20	3.78	1.18
URMM	420	315	0.0016	0.0032	0.0080	0.0187	0.50	1.0	1.01	0.97	2.52	0.90	5.88	0.88
МН	120	120	0.0032	0.0064	0.0192	0.0560	0.38	1.12	0.77	1.10	2.30	0.95	6.72	0.97

Figure: Selection of displacement limits from HAZUS Table 5-22 for the appropriate building typology.

Spectral displacement at DS1	$S_{d,DS1} = 0.0254 \cdot 0.32$ $S_{d,DS1} = 0.0081 m$
Spectral displacement at DS2	$S_{d,DS2} = 0.0254 \cdot 0.65$ $S_{d,DS2} = 0.0165 m$
Spectral displacement at DS3	$S_{d,DS3} = 0.0254 \cdot 1.62$ $S_{d,DS3} = 0.0411 m$
Spectral displacement at DS3	$S_{d,DS4} = 0.0254 \cdot 3.78$ $S_{d,DS4} = 0.0960 m$

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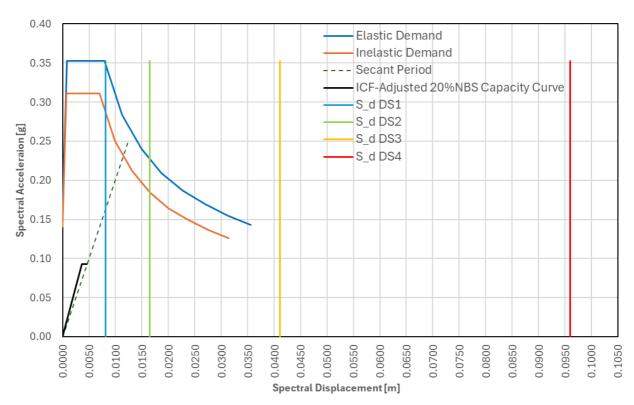


Figure: Comparison of structural backbone to HAZUS damage state spectral displacements.

#### 5. Structural Damage State Spectral Acceleration Intensity

In this stage, the comparisons between spectral displacement limits and spectral acceleration are made for the structure. The higher damage state spectral displacement thresholds are often well above the ultimate spectral displacement of the structure. In these cases, an 'effective' ductility can be assumed. In reality, the structure will be reducing in capacity as significant damage occurs.

There are a number of complex relationships formulated between the structural pushover backbone and the true capacity as determined from an incremental dynamic analysis. We will retain the simple relationships of equal displacement and equal energy to estimate the structure's spectral acceleration capacity.

For damage state DS1, the equivalent elastic spectral acceleration is calculated below.

Slope of the elastic curve

$$K_{elastic} = \frac{S_a}{S_{dy}}$$

$$K_{elastic} = \frac{0.093}{0.0037}$$

$$K_{elastic} = 25.2$$

Effective ductility to reach damage state

$$\begin{split} \mu_{eff} &= \frac{S_{d,DS1}}{S_{dy}} \\ \mu_{eff} &= \frac{0.0081}{0.0037} \\ \mu_{eff} &= 2.2 \end{split}$$

Area beneath the inelastic backbone beyond the yield point.

$$A_{plastic} = (S_{d,DS1} - S_{dy}) \cdot S_a$$
  
 $A_{plastic} = (0.0081 - 0.0037) \cdot 0.093$   
 $A_{plastic} = 4.12 \times 10^{-6}$ 



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Area beneath the elastic backbone

$$A_{elastic} = S_a \cdot \frac{S_{dy}}{2}$$

$$A_{elastic} = 0.0093 \cdot \frac{0.0037}{2}$$

$$A_{elastic} = 1.72 \times 10^{-6}$$

Total area beneath backbone

$$\begin{split} A_{backbone} &= A_{plastic} + A_{elastic} \\ A_{backbone} &= 4.12 \times 10^{-6} + 1.72 \times 10^{-6} \\ A_{backbone} &= 5.84 \times 10^{-6} \end{split}$$

The area of the backbone equals the area of the equivalent elastic curve Rearranging for spectral displacement

$$A_{backbone} = S_{d,equiv} \cdot \frac{S_{a,equiv}}{2}$$

$$S_{d,equiv} = 2 \cdot \frac{A_{backbone}}{S_{a,equiv}}$$

The slope of the curve is the elastic slope

$$S_{a,equiv} = K_{elastic} \cdot S_{d,equiv}$$

Rearranging for spectral displacement

$$S_{d,equiv} = \frac{S_{a,equiv}}{K_{elastic}}$$

Combining the two equations

$$\begin{aligned} 2 \cdot \frac{A_{backbone}}{S_{a,equiv}} &= \frac{S_{a,equiv}}{K_{elastic}} \\ S_{a,equiv} &= \sqrt{2 \cdot A_{backbone} \cdot K_{elastic}} \end{aligned}$$

Rearranging for spectral acceleration yields the equivalent elastic spectral acceleration

$$S_{a,equiv} = \sqrt{2 \cdot 5.84 \times 10^{-6} \cdot 25.2}$$
  
$$S_{a,equiv} = 0.0171 \ g$$

Repeating the process for each damage state gives the following values.

Damage State	Equivalent Elastic Spectral Acceleration [g]
DS1	0.171
DS2	0.262
DS3	0.429
DS4	0.663

These can be visualized as shown in the figures below (figure values are approximate only).

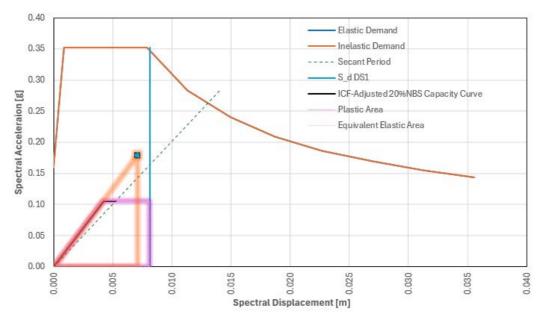


Figure: Graphical representation of equal energy method to determine DS1 equivalent spectral acceleration intensity.

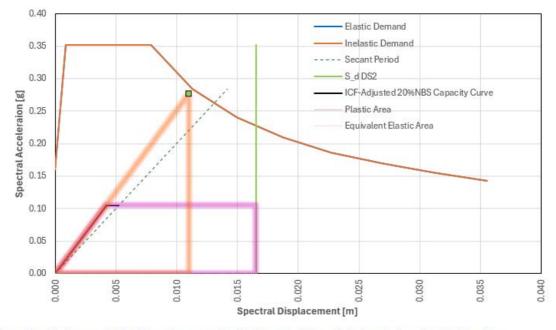


Figure: Graphical representation of equal energy method to determine DS2 equivalent spectral acceleration intensity.

Figure: Graphical representation of equal energy method to determine DS2 equivalent spectral acceleration intensity.

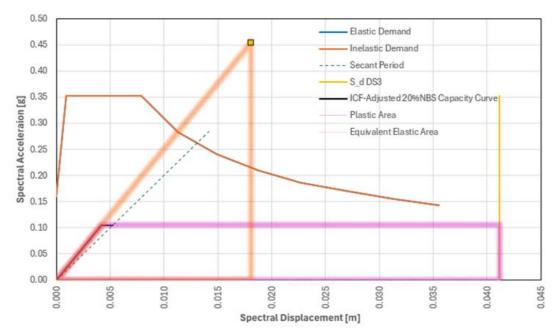


Figure: Graphical representation of equal energy method to determine DS3 equivalent spectral acceleration intensity.

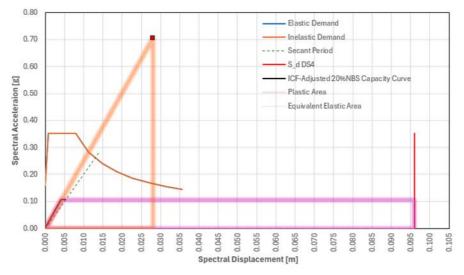


Figure: Graphical representation of equal energy method to determine DS4 equivalent spectral acceleration intensity.

#### 6. Fragility Curves

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For this example of one building, the median spectral acceleration for each fragility curve is equal to the equivalent elastic spectral acceleration capacity of this single building. For the actual calculation, all of the values of spectral acceleration for buildings in a specific city and of a specific typology would be averaged to determine the median collapse fragility spectral acceleration values.

For dispersion, the value of 0.64 shown in HAZUS is taken as the dispersion of the fragility curves.

Table: Exemplar fragility curve based on structural calculations for one building (actual calculation would be based on whole subset of the earthquake-prone building register).

Damage State	Median	Dispersion (beta)
DS1	0.171	0.64
DS2	0.262	0.64
DS3	0.429	0.64
DS4	0.663	0.64

#### 7. Normalization of Structural Period

In order to make a comparison between a range of buildings of different periods of vibration, some method of normalization is required. Other observed methods such as Hulsey et al. (2024) have been to use a ratio of SA for the damage state against an SA capacity as per the code. Here, we have chosen to use a normalized SA at a benchmark period as this is easier to compare back to the hazard presented on the GNS Webtool for the hazard. Normalize the individual  $S_a(T_1)$  intensity associated with each damage state for the individual structure to a consistent benchmark  $S_a(T_{benchmark})$ .

Benchmark period	T=0.4~s
Spectral shape factor of benchmark period	$C_h(T_{benchmark}) = 2.36$
Spectral shape factor of structural period	$C_h(T_1) = 2.36$
Ratio of benchmark to structural period spectral accelerations	$R_{normal} = 1.0$

In this case, because only one building is used.



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#### Iteratively improve structural backbones to achieve 34% and 67%

To account for strengthening, the structural backbones are adjusted in accordance with the expected result of the retrofits to that structure. This may improve force or ductility capacity of the structure by some factor. This process is iterated until the targeted %NBS is reached. Then, the same process of converting backbones to equivalent spectral acceleration values at  $T_{benchmark}$  is completed.

The below calculation shows the process undertaken to determine the backbone for a 67% strengthened structure.

Strengthening level

$$\%NBS_{str} = 67\%$$

Relative degree to which strengthening includes the increase of force capacity.

$$F_F = 1.0$$

Relative degree to which strengthening includes the increase of displacement capacity.

$$F_{u} = 1.0$$

Maximum ductility that the structure can  $\mu_{max} = 1.25$ have after strengthening

$$\mu_{max} = 1.25$$

In other words, the structure's ductility cannot be improved beyond nominally ductile.

Based on these value's increase force by some increment and ductility by some other increment and observe the changes to the structural capacity curve and inelastic structural demand curve.

No improvements in ductility are possible as the structure is already nominally ductile. Therefore, only the force increment could be improved. After successive iterations, the force increment leading to a 67% backbone was found to be

Force increment used to yield a 67%

$$inc_F = 4.5$$

backbone.

Ductility increment used to yield a 67%

backbone.

$$inc_{u} = 1.0$$

New ductility after incrementation

$$\mu_{new} = inc_{\mu} \cdot \mu$$

$$\mu_{new} = 1.0 \cdot 1.25$$

New ultimate spectral displacement after incrementation

$$S_{du,new} = \mu_{new} \cdot S_{du}$$

 $S_{du.new} = 1.25 \cdot 0.0037$  $S_{du.new} = 0.0046 m$ 

New spectral acceleration after incrementation

$$S_{a.new} = inc_F \cdot S_a$$

This value is only used for intersection with the demand curve, it is not the backbone

$$S_{a,new} = 4.5 \cdot 0.093$$
  
 $S_{a,new} = 0.418 g$ 

capacity

New hysteretic damping as a result of ductility

$$\xi_{hy,new} = 2\%$$

EAG Table C2D.1

New system damping as a result of ductility

$$\xi_{sys,new} = 7\%$$

New spectral damping reduction factor

$$k_{\xi} = 0.88$$

New elastic period of vibration

$$T_{1,new} = \sqrt{4\pi^2 \cdot \frac{S_{dy,new}}{9.81 \cdot S_{a,new}}}$$

$$T_{1,new} = \sqrt{4\pi^2 \cdot \frac{0.0037}{9.81 \cdot 0.418}}$$

$$T_{1,new} = 0.189 \text{ s}$$

New secant period of vibration

$$T_{s,new} = \sqrt{4\pi^2 \cdot \frac{S_{du,bew}}{9.81 \cdot S_{a,new}}}$$

$$T_{s,new} = \sqrt{4\pi^2 \cdot \frac{0.0046}{9.81 \cdot 0.418}}$$

$$T_{s,new} = 0.211 \, s$$

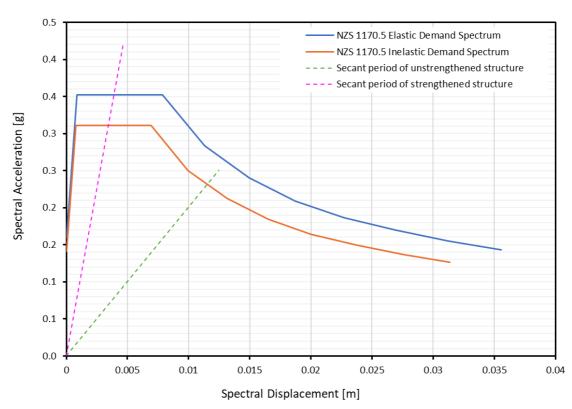


Figure: Change in secant period as a result of strengthening by improving force capacity.

Having identified the secant period, the 100%NBS backbone can be produced.

Spectral acceleration of a 100%NBS structure

$$S_{a,100} = 0.311 g$$

Spectral displacement of a 100%NBS structure

$$\begin{split} S_{du,100} &= 9.81 \cdot S_{a,100} \cdot \frac{T_s^2}{4\pi^2} \\ S_{du,100} &= 9.81 \cdot 0.311 \cdot \frac{0.211^2}{4\pi^2} \\ S_{du,100} &= 0.0034 \, m \end{split}$$

Spectral acceleration of the strengthened 67%NBS structure

$$S_{a,nbs} = \%NBS \cdot S_{a,100}$$

$$S_{a,nbs} = 67\% \cdot 0.311$$
  
 $S_{a,nbs} = 0.209 g$ 

Spectral displacement of the strengthened 67%NBS structure

$$S_{a,nbs} = \%NBS \cdot S_{du,100}$$

$$S_{du,nbs} = 67\% \cdot 0.0034$$
  
 $S_{a,nbs} = 0.0023 \ g$ 

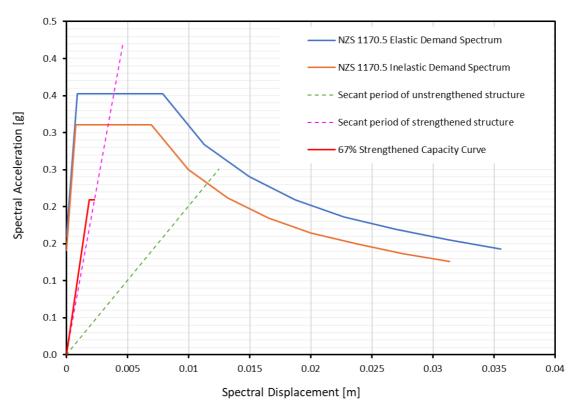


Figure: Structural capacity backbone for 67% strengthening backbone

Similar to the unstrengthened case, the steps of improving the backbone by the inherent capacity factor and establishing an equivalent elastic spectral acceleration were performed. The resulting elastic spectral accelerations are shown in the below plot.

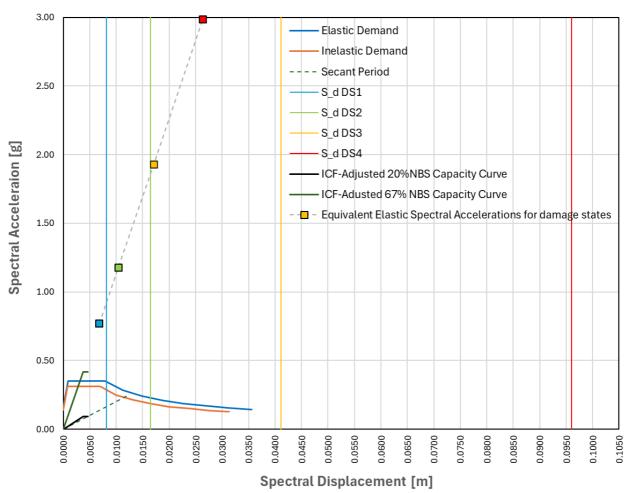


Figure: Equivalent elastic spectral accelerations for damage states

Finally, the spectral accelerations can be normalized to the benchmark period.

Benchmark period T = 0.4 s

Spectral shape factor of benchmark  $C_h(T_{benchmark}) = 2.36$  period

Spectral shape factor of structural  $C_h(T_1) = 2.93$  period

Ratio of benchmark to structural period  $R_{normal} = 0.81$  spectral accelerations

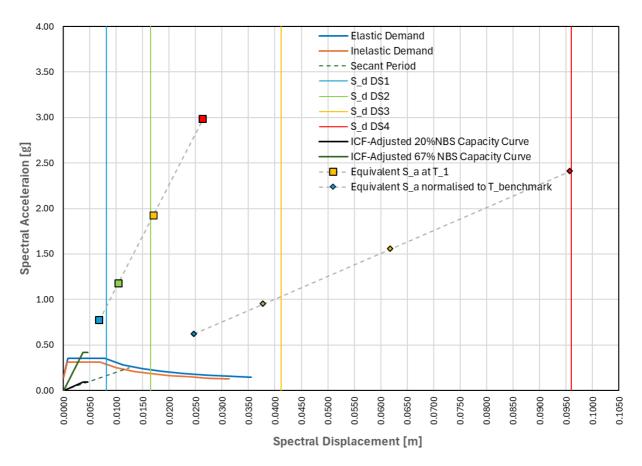


Figure: Equivalent elastic spectral accelerations for damage states normalized to the benchmark period. Diamonds represent the accelerations used as the median fragility for each damage state.

#### Therefore, the strengthened fragility curve is:

Damage State	Median	Dispersion (beta)
DS1	0.62	0.64
DS2	0.95	0.64
DS3	1.56	0.64
DS4	2.41	0.64



#### **Calculation Sheet**

Page Nº:

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#### 9. Identifying the new hazard intensity for given return period

Note values in the below calculation slightly misalign with the previous sections but the methodology is consistent.

RP = 500 Return period

APE = 0.002 Annual probability of exceedance

(approximate)

Dunedin for APoE 1:2500 to 1:100 below: (short periods)

Dunedin (Vs30= 350m/s)

	PoE	0.4s	0.7s	1s	1.5s	2s
100	0.01	0.226	0.155	0.116	0.076	0.055
250	0.004	0.377	0.263	0.198	0.129	0.097
500	0.002	0.535	0.376	0.284	0.187	0.139
1000	0.001	0.744	0.528	0.399	0.263	0.198
2500	0.0004	1.122	0.814	0.618	0.405	0.304

T = 0.4 sec

Sa = 0.53g

# 10. Determine the relative likelihoods of different damage states based on earthquake scenario intensity

From previous page:

S\_a = 0.53 g

(Fragility data for unstrengthened 20%NBS)

Table: The probability of each damage state exceedance

DS	P [DS > ds					
	IM > im]	Table: Frag	ility curve	CDF visualis	ed	
DS0	100%	SA(T_avg) Intensity	DS1	DS2	DS3	DS4
DS1	80%	0.225	0.302	0.128	0.030	0.005
DS2	59% ◀	0.375	0.610	0.369	0.140	0.039
DS3	30%	0.53 0.74	0.794	0.581 0.766	0. <del>294</del> 0.492	- 0.112 0.244
DS4	11.8%	1.12	0.977	0.915	0.735	0.481

Based on these probabilities, the relative likelihood that a building is in a given damage state as a result of the scenario earthquake is calculated. This is the probability that the damage state is exceeded minus the probability of any higher damage states being exceeded.

Table: The relative likelihood of a given damage state

DS	P[DS>ds	P [DS = ds
	IM > im]	IM > im]
DS0	100.0%	24.3%
DS1	75.7%	22.5%
DS2	53.3%	28.0%
DS3	25.3%	16.3%
DS4	9.0%	9.0%



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Table: Fragility based on average of only one building in

this	exam	р	le
D.C.			

DS	median	beta	
DS1	0.179	0.64	
DS2	0.276	0.64	
DS3	0.455	0.64	
DS4	0.705	0.64	

#### Table: Probabilities at given intensities

DS	DS   IM	DS > ds   IM	
DS0	1	6%	
DS1	0.96	13%	alpha
DS2	0.85	27%	Z
DS3	0.60	26%	У
DS4	0.34	28%	Х

#### With the following formular.

DS | IM for DS0 = 1.0

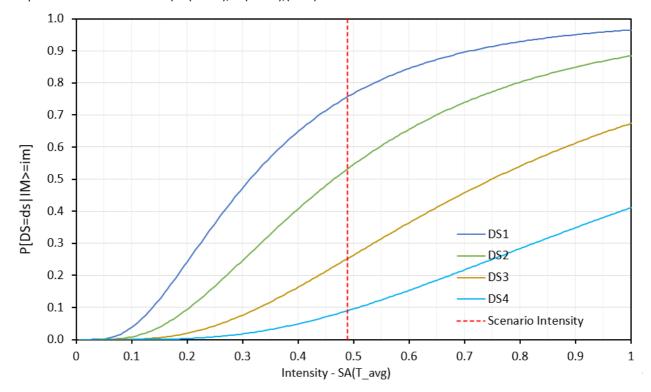
DS | IM for DS1 = NORM.DIST(LN(Sa),LN(median\_DS1),Beta\_DS1, TRUE,0

DS | IM for DS1 = NORM.DIST(LN(0.226),LN(0.179),(0.64) = 0.94

DS | IM for DS2 = NORM.DIST(LN(0.226),LN(0.276),(0.64) = 0.81

DS | IM for DS3 = NORM.DIST(LN(0.226),LN(0.455),(0.64) = 0.54

DS | IM for DS4 = NORM.DIST(LN(0.226),LN(0.705),(0.64) = 0.28



This can be interpreted as, for this design level earthquake scenario, there being an approximately x% chance that the earthquake-prone building totally collapses, a y% chance that the building partially collapses, a z% chance of light failure and only an alpha% chance of minor damage.

#### 11. Loss

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In the actual loss calculation, each building is assigned a ground floor area and occupancy type. The occupancy density of each building type has been provided by GNS Science \*REF\*. Several cases have been created to account for different times of day which impact the relative occupancy density of different building types.

For this example calculation, the following parameters have been used as a demonstration:

Occupancy type	COM13	User chosen
Ground floor area	$GFA = 300 m^2$	User chosen
Time of day	10 am (day)	User chosen
Proportion of peak occupancy	$R_{peak} = 0.9$	Provided by GNS Science
Occupancy density	$ \rho_{occ} = 1/14  people/m^2 $	Provided by GNS Science
Outside occupancy modifier	$k_{outside} = 1.1$	Provided by GNS Science

#### **Human Consequences**

For human consequences, the occupancy density at the time of the event and the ground floor area of the structure must be factored into the final loss. In this example calculation, the ground floor area is of one building only, but in the whole calculation, the total ground floor area of all buildings of the occupancy type for the given case (of location, typology, time of day, etc.) must be considered.

Here is an example of the calculation for the CS5 (in death equivalents) given that DS4 (complete collapse) occurs.

Consequence value 
$$C = P[CS5|ds = DS4] \cdot R_{peak} \cdot \rho_{occ} \cdot k_{outside} \cdot GFA$$
 
$$C = 0.3 \cdot 0.9 \cdot \frac{1}{14} \cdot 1.1 \cdot 300$$
 
$$C = 6.4 \ death \ equivalents$$

#### **Human Losses**

From earlier steps, the relative likelihood of damage states occurring given an event of a given severity is provided. Therefore, using CS5 as an example, the CS5 consequence for the given scenario can be determined.

Damage State	Consequence values (death equivalents given that damage state definitely occurs)	Probability of the given damage state occurring in the scenario $P[ds]$	Expected loss in the given scenario due to given damage state
DS1	0	13%	0
DS2	0	27%	0
DS3	2.1	26%	0.6
DS4	6.4	28%	1.8

The sum of expected losses across all damage states provides the total expected loss of the scenario.

CS5 expected loss across all damage states

$$L = \sum_{DSX=DS1}^{DS4} C[ds = DSX]$$

$$C = 0 + 0 + 0.6 + 1.8$$

$$C = 2.4 \ death \ equivalents$$

This process is repeated across a range of consequences.

Table: Losses for single structure example.

Consequence Type	Damage State	Consequence values (death equivalents given that damage state definitely occurs) (units specific to consequence)	Probability of the given damage state occurring in the scenario $P[ds \ DSX]$	Expected loss in the given scenario due to given damage state (units specific to consequence)
CS2	DS1	0.20	13%	0.03
CS2	DS2	0.80	27%	0.22
CS2	DS3	1.40	26%	0.37
CS2	DS4	1.00	28%	0.28
CS3	DS1	0.0	13%	0.00
CS3	DS2	0.0	27%	0.01
CS3	DS3	0.8	26%	0.20
CS3	DS4	3.2	28%	0.92
CS4	DS1	0.0	13%	0.00
CS4	DS2	0.0	27%	0.00
CS4	DS3	1.1	26%	0.29
CS4	DS4	3.3	28%	0.93
CS5	DS1	0.0	13%	0.00
CS5	DS2	0.0	27%	0.00
CS5	DS3	2.1	26%	0.55
CS5	DS4	6.4	28%	1.80
CS2_USAR	DS1	0.2	13%	0.03
CS2_USAR	DS2	0.8	27%	0.22
CS2_USAR	DS3	1.4	26%	0.37
CS2_USAR	DS4	1.0	28%	0.28
CS3_USAR	DS1	0.0	13%	0.00
CS3_USAR	DS2	0.0	27%	0.01
CS3_USAR	DS3	0.8	26%	0.20
CS3_USAR	DS4	3.2	28%	0.92
CS4_USAR	DS1	0.0	13%	0.00
CS4_USAR	DS2	0.0	27%	0.00
CS4_USAR	DS3	1.1	26%	0.29
CS4_USAR	DS4	3.3	28%	0.93
CS5_USAR	DS1	0.0	13%	0.00
CS5_USAR	DS2	0.0	27%	0.00
CS5_USAR	DS3	2.1	26%	0.55
CS5_USAR	DS4	6.4	28%	1.80
DR	DS1	0.1	13%	0.01
DR	DS2	0.3	27%	0.08
DR	DS3	0.8	26%	0.21
DR	DS4	1.0	28%	0.28
Carbon repair	DS1	0.1	13%	0.01
Carbon repair	DS2	0.3	27%	0.08
Carbon repair	DS3	0.8	26%	0.21

III Beca		Calculation Sheet		Page Nº:	25 of 11
Carbon repair	DS4	1.0	28%		0.28
BD direct	DS1	1.0	13%		0.13
BD direct	DS2	270.0	27%		73
BD direct	DS3	365.0	26%		95
BD direct	DS4	365.0	28%		103
BD indirect	DS1	1.0	13%		0.13
BD indirect	DS2	270.0	27%		73
BD indirect	DS3	365.0	26%		95
BD indirect	DS4	365.0	28%		103

Table: Aggregated losses for single structure example.

Damage State	Expected Loss
CS2	0.9
CS3	1.1
CS4	1.2
CS5	2.4
CS2_USAR	0.9
CS3_USAR	1.1
CS4_USAR	1.2
CS5_USAR	2.4
DR	0.6
Carbon repair	0.6
BD direct	270
BD indirect	270

#### 12. Costed Loss

Given the costs for the individual case, and the losses established in the previous sections, the costs of each consequence can be calculated.

To complete the example with CS5, the costed loss is:

Costed loss CL = L \* Cost

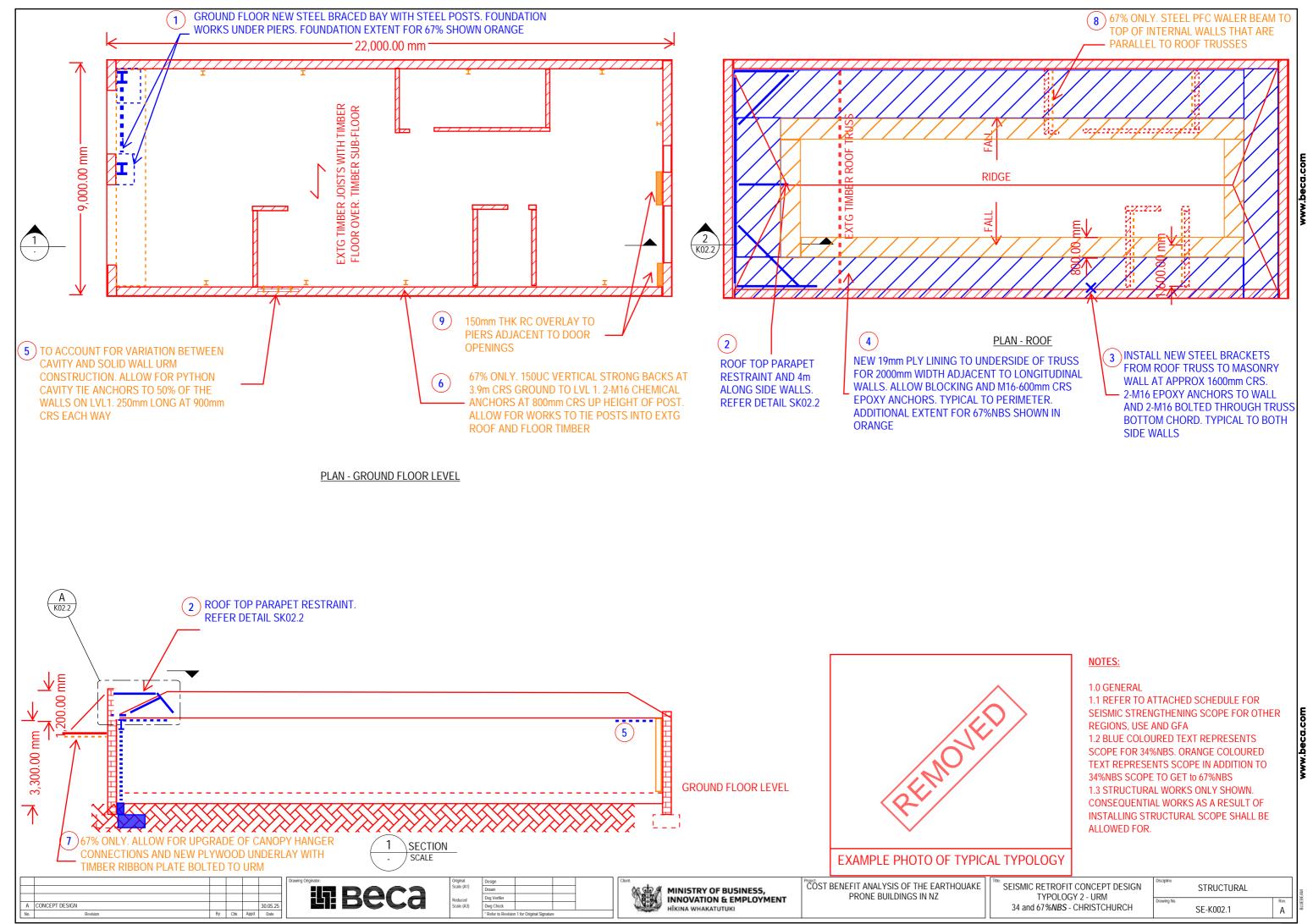
CL = 2.4 \* \$17.5M

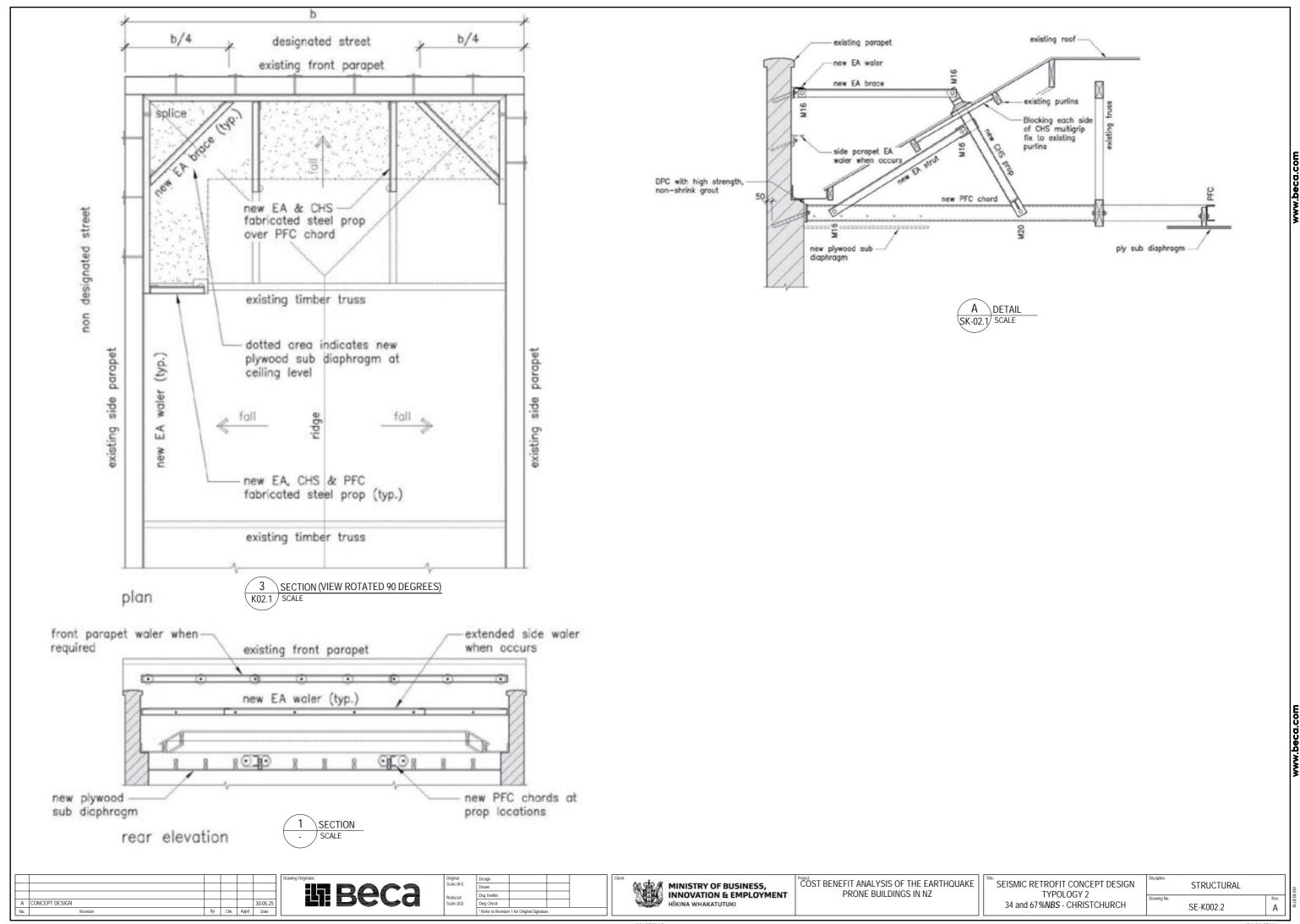
CL = \$41.3M

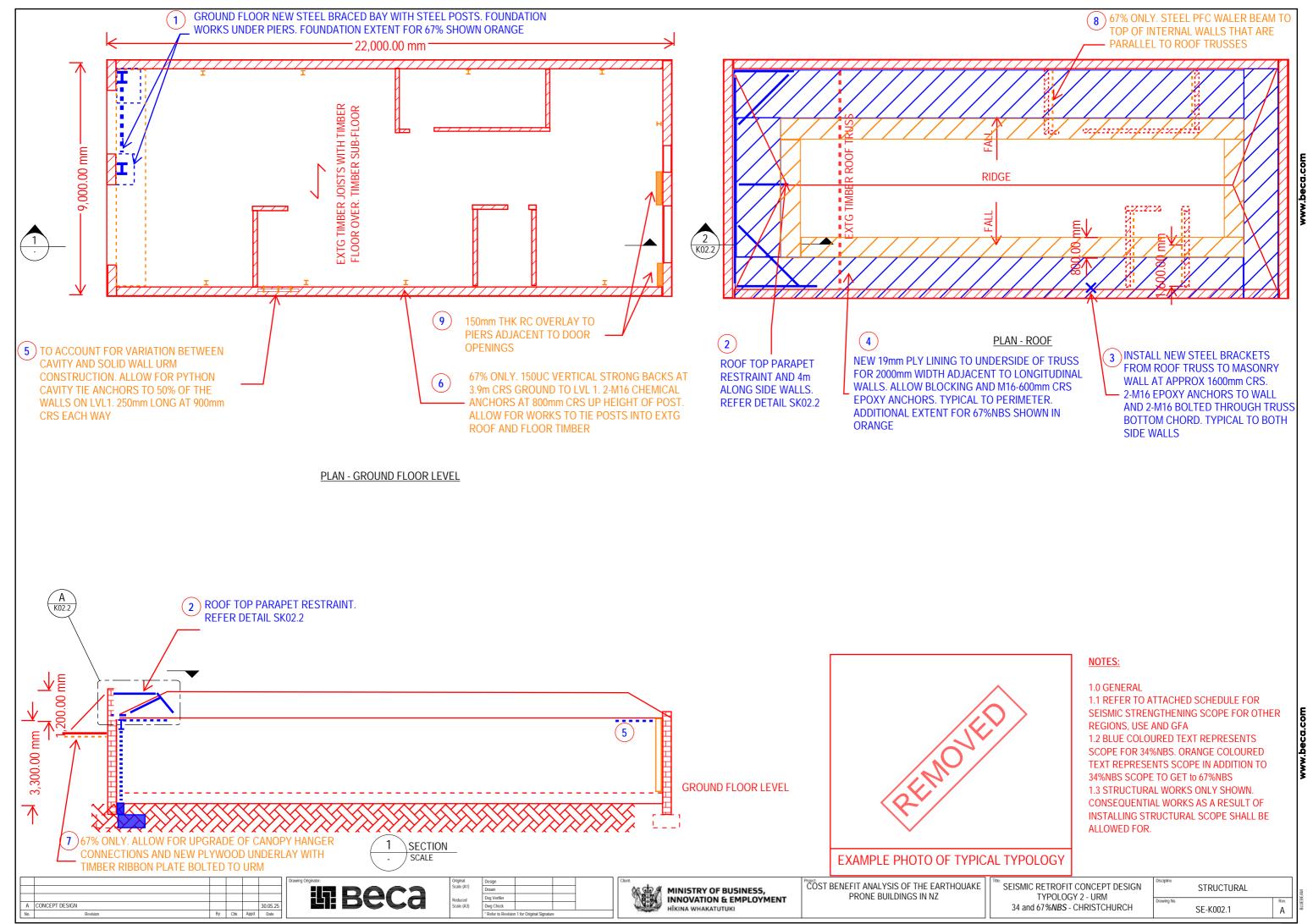


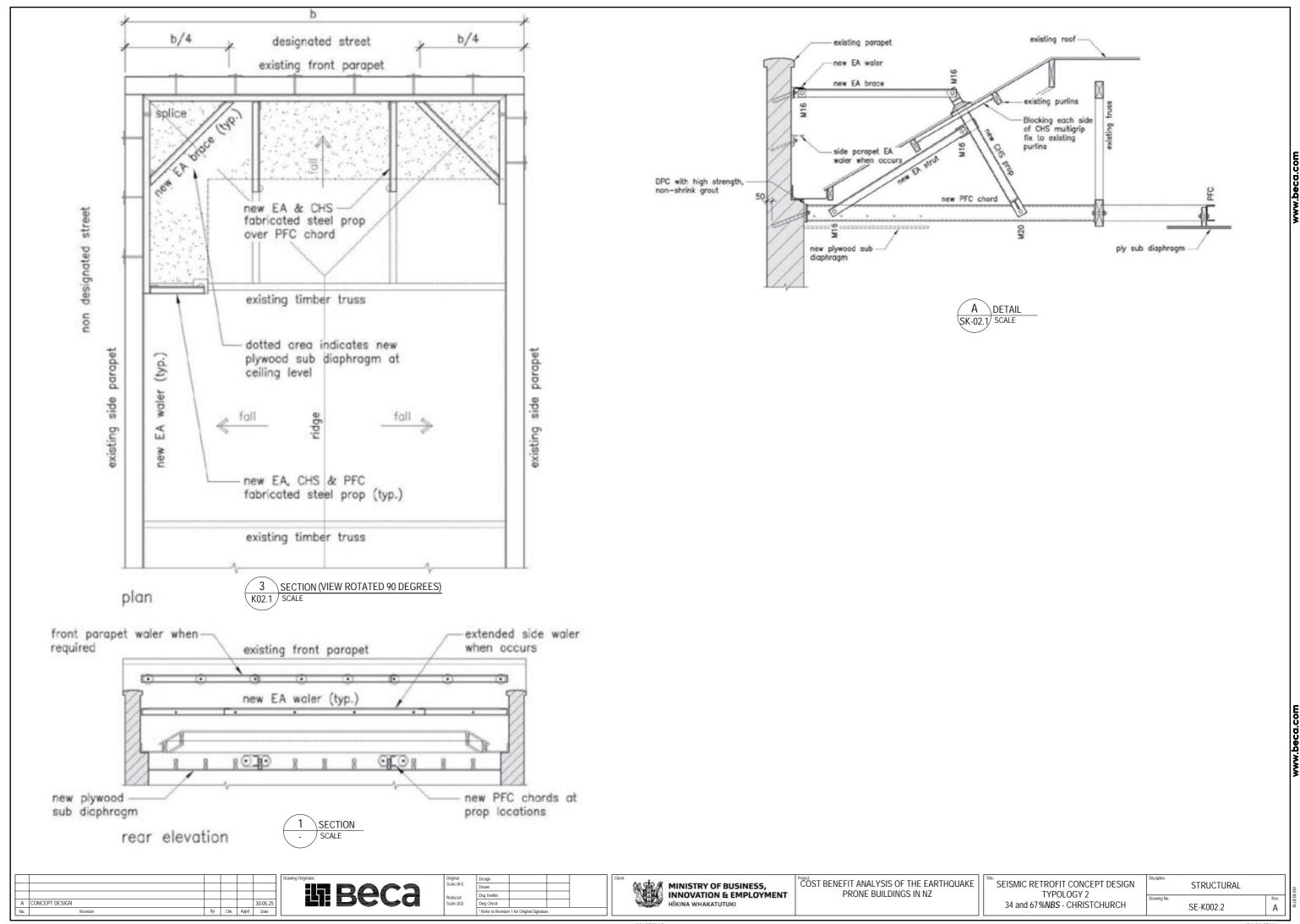
Appendix D
Seismic Retrofit Concepts
For Reference Buildings

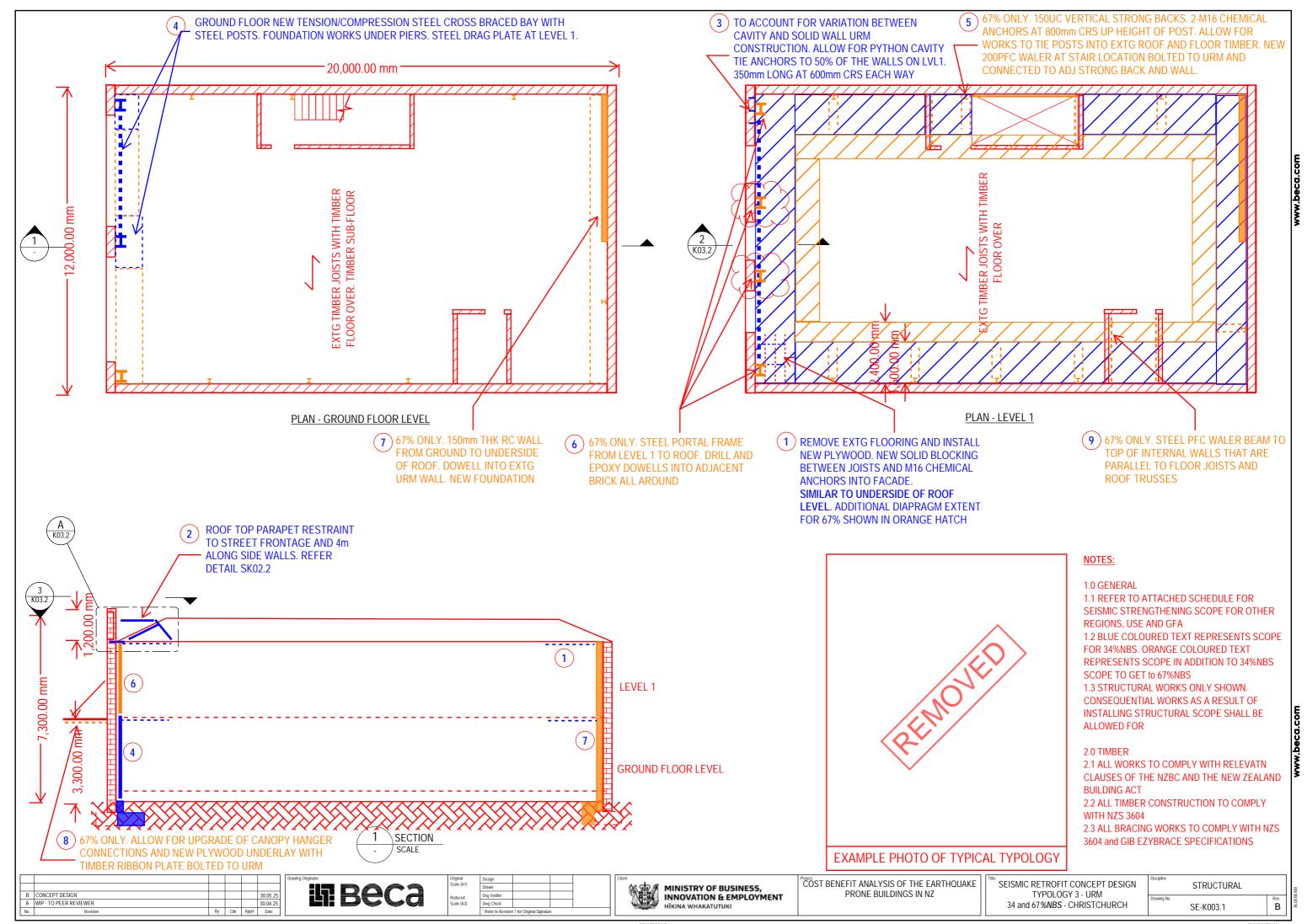


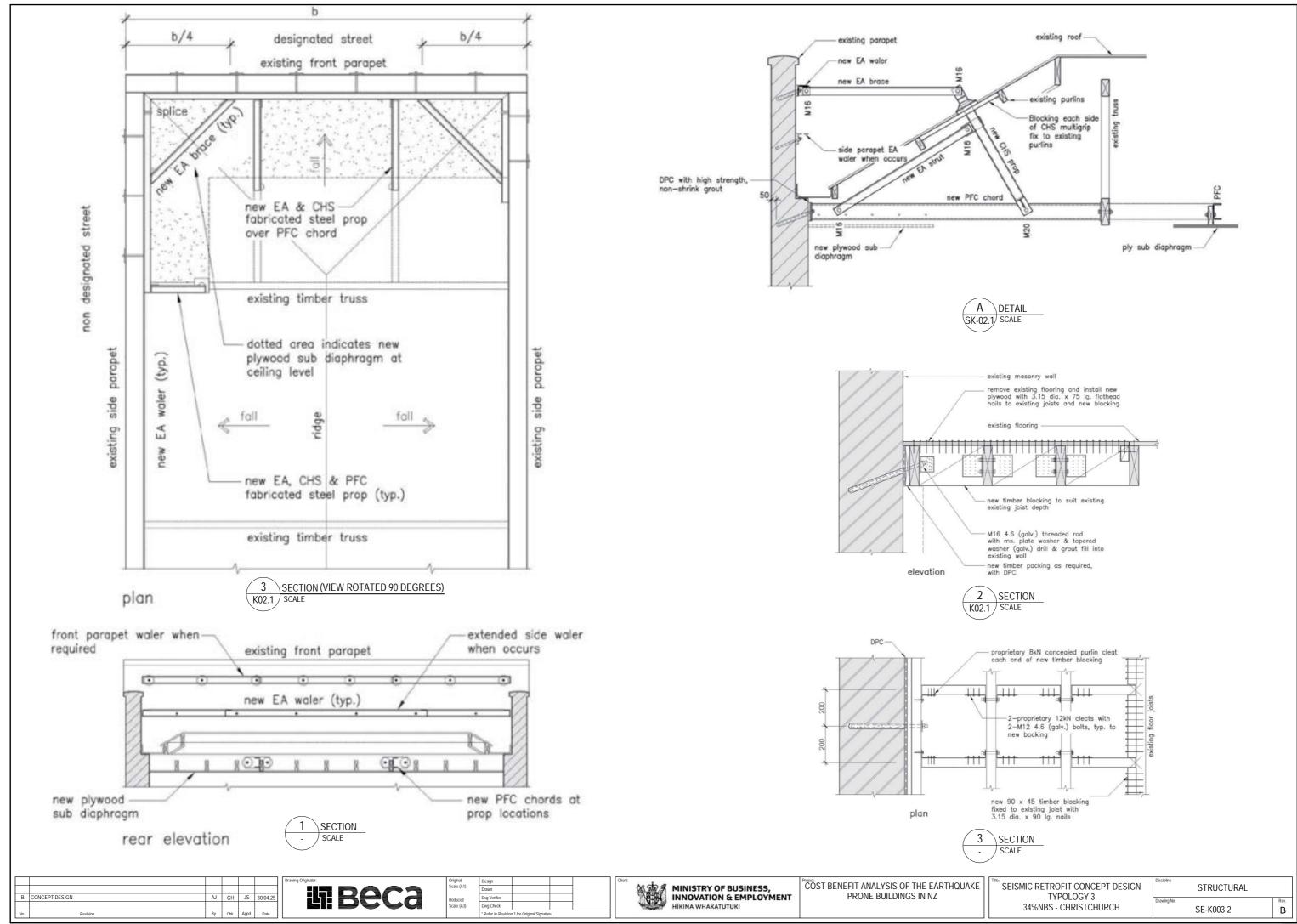


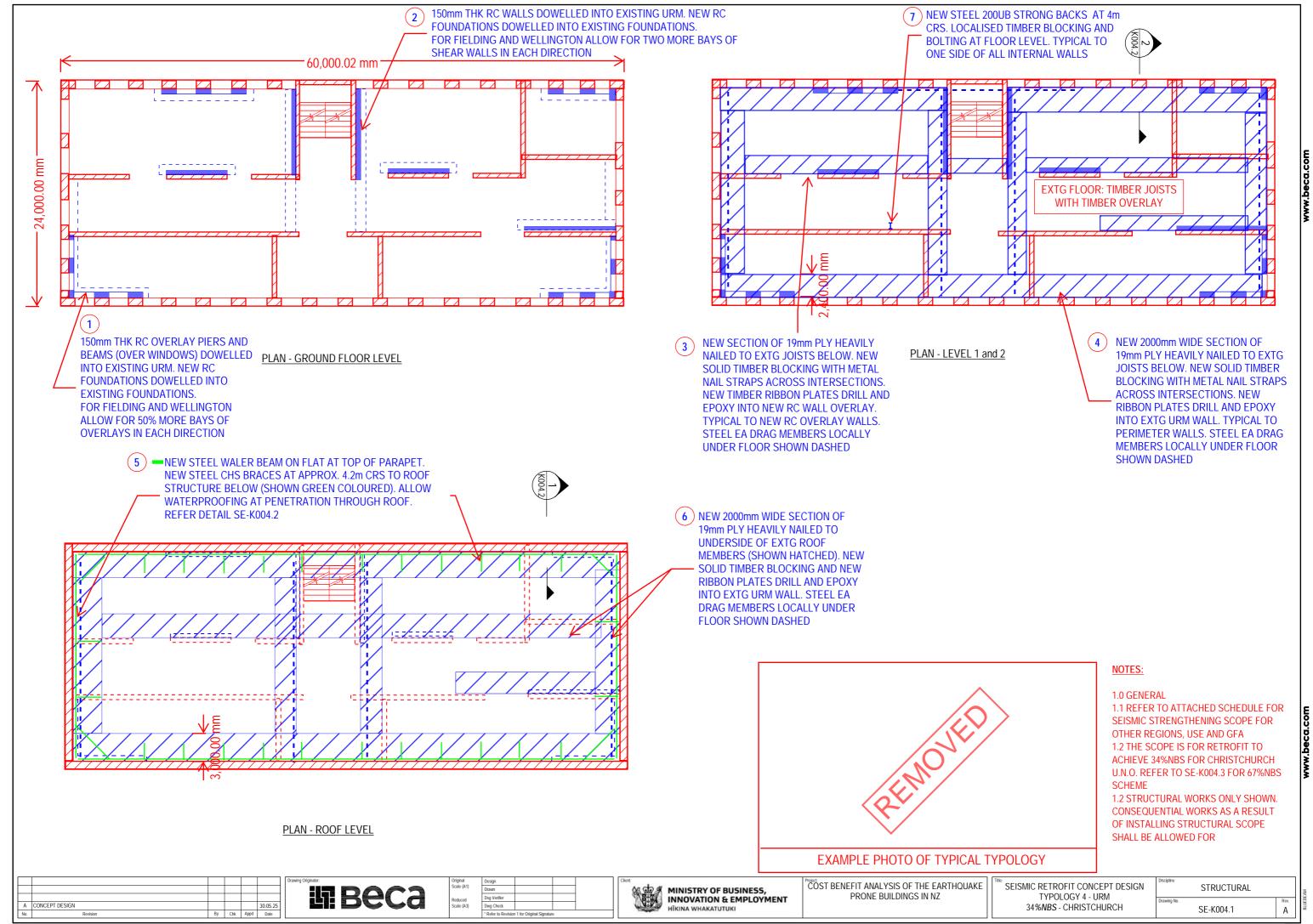








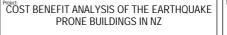


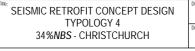


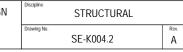


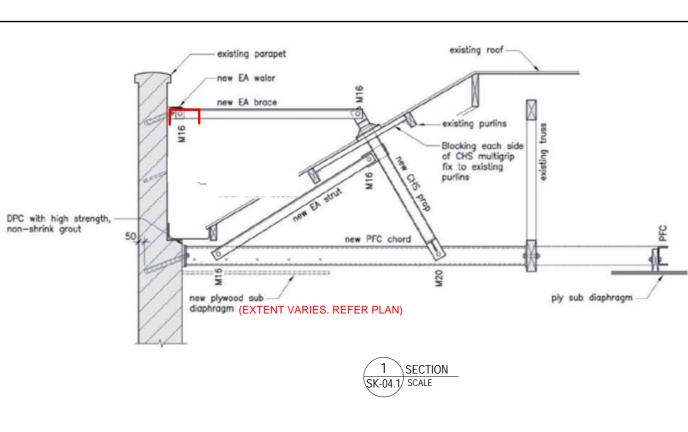


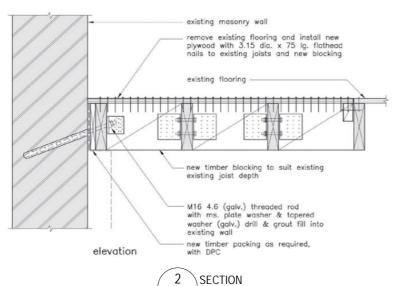


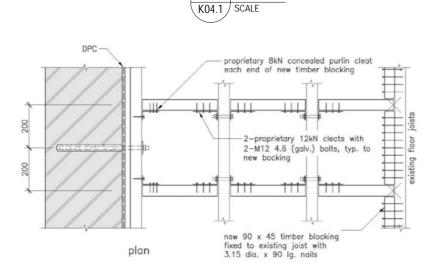










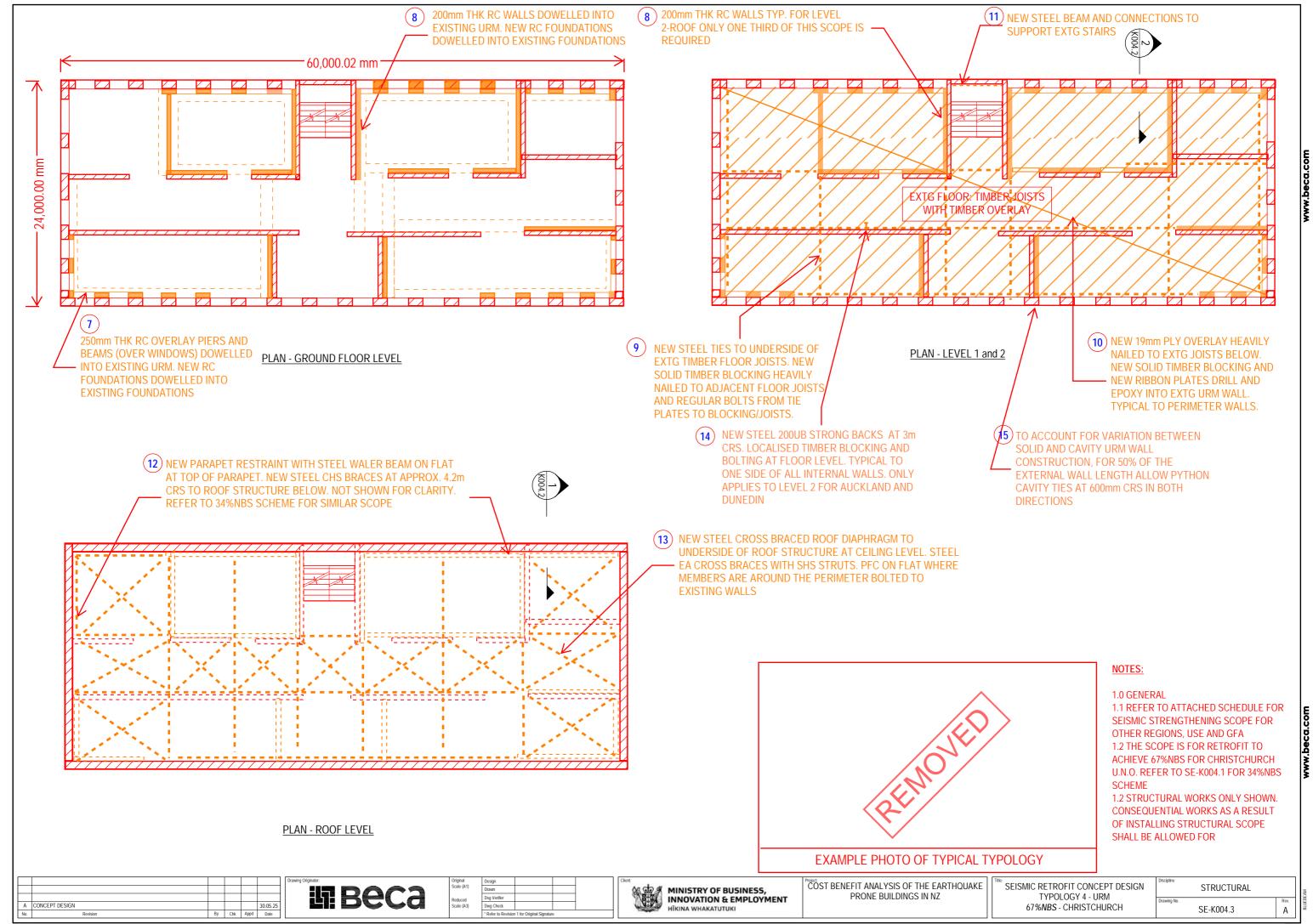


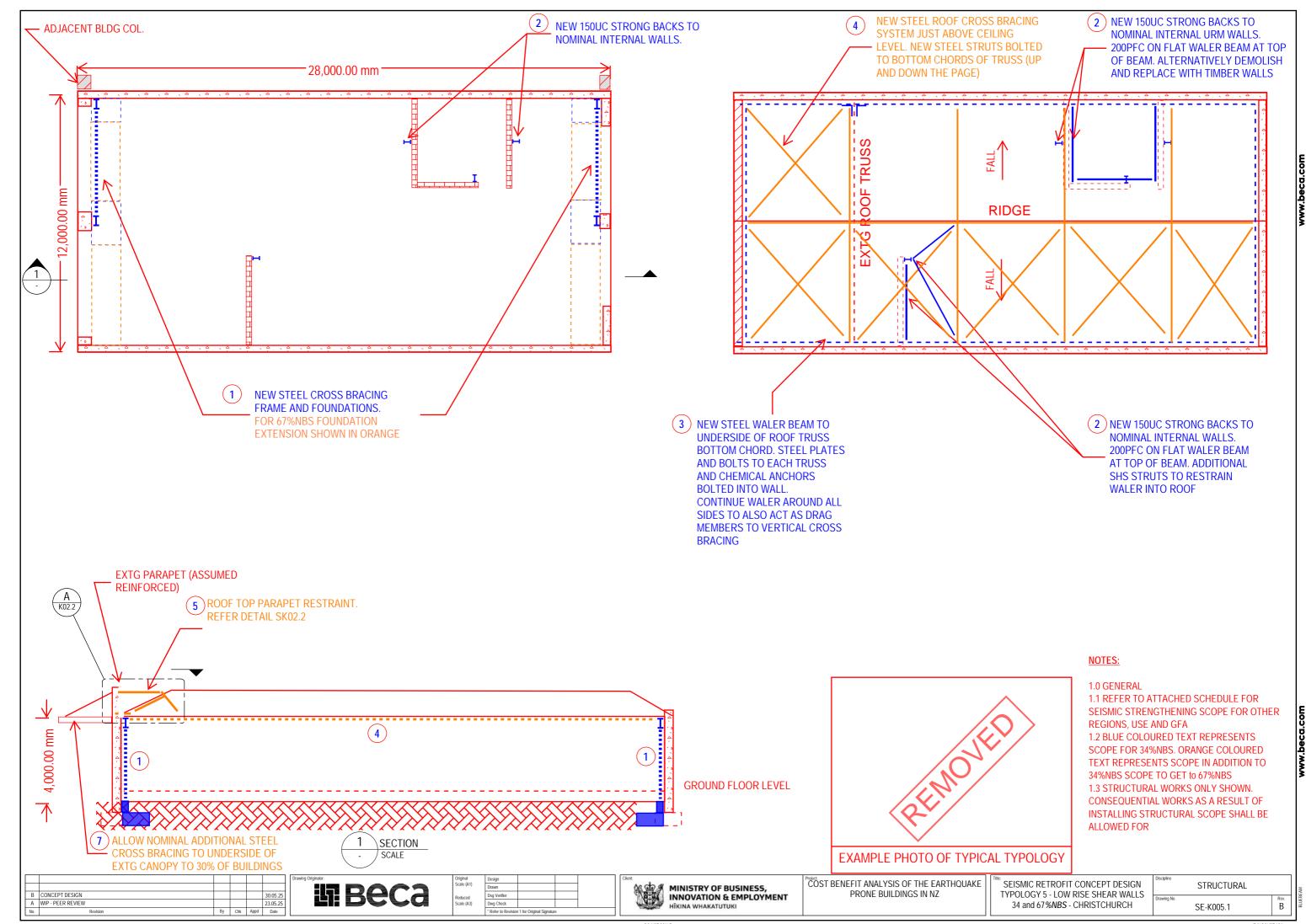
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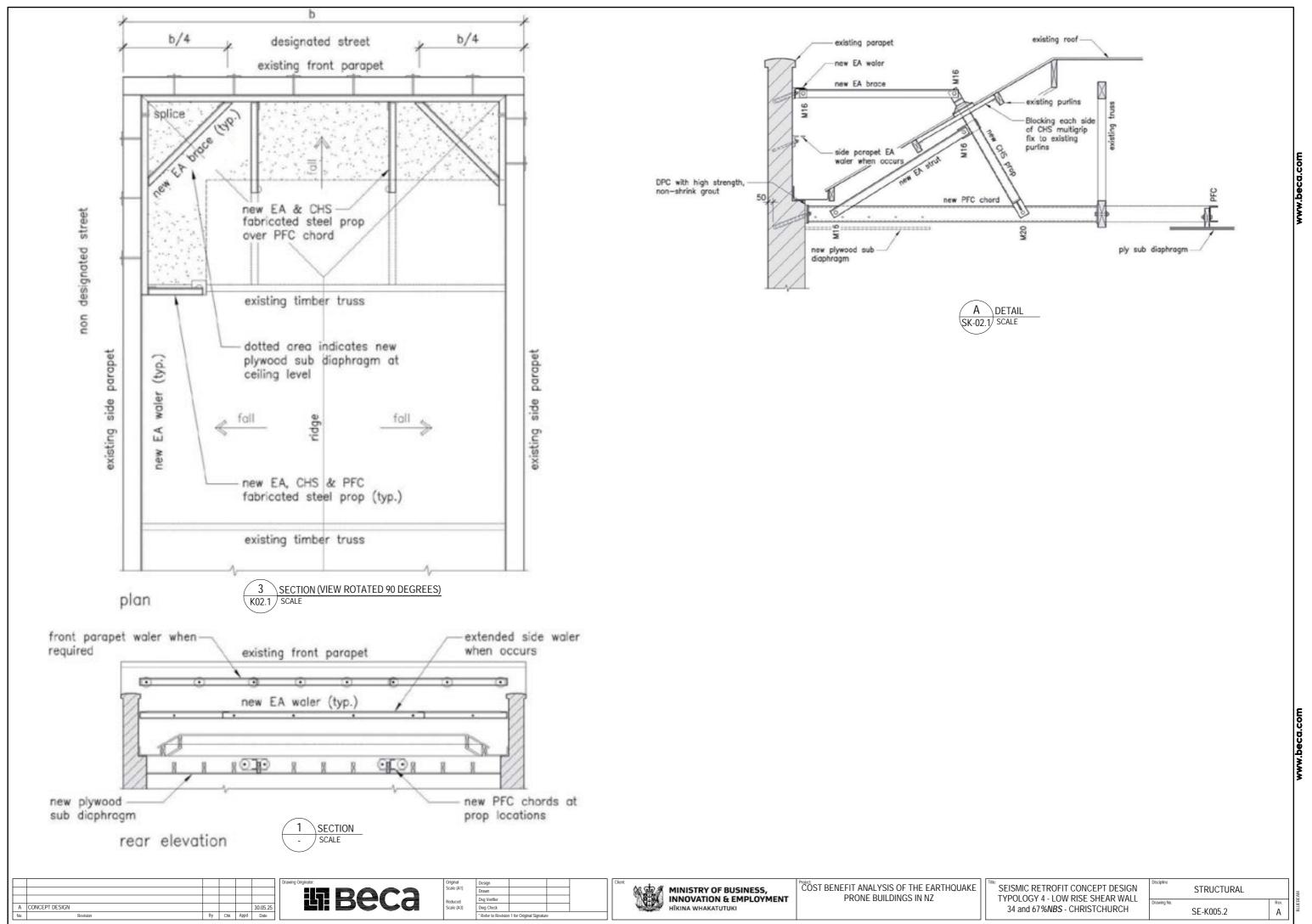
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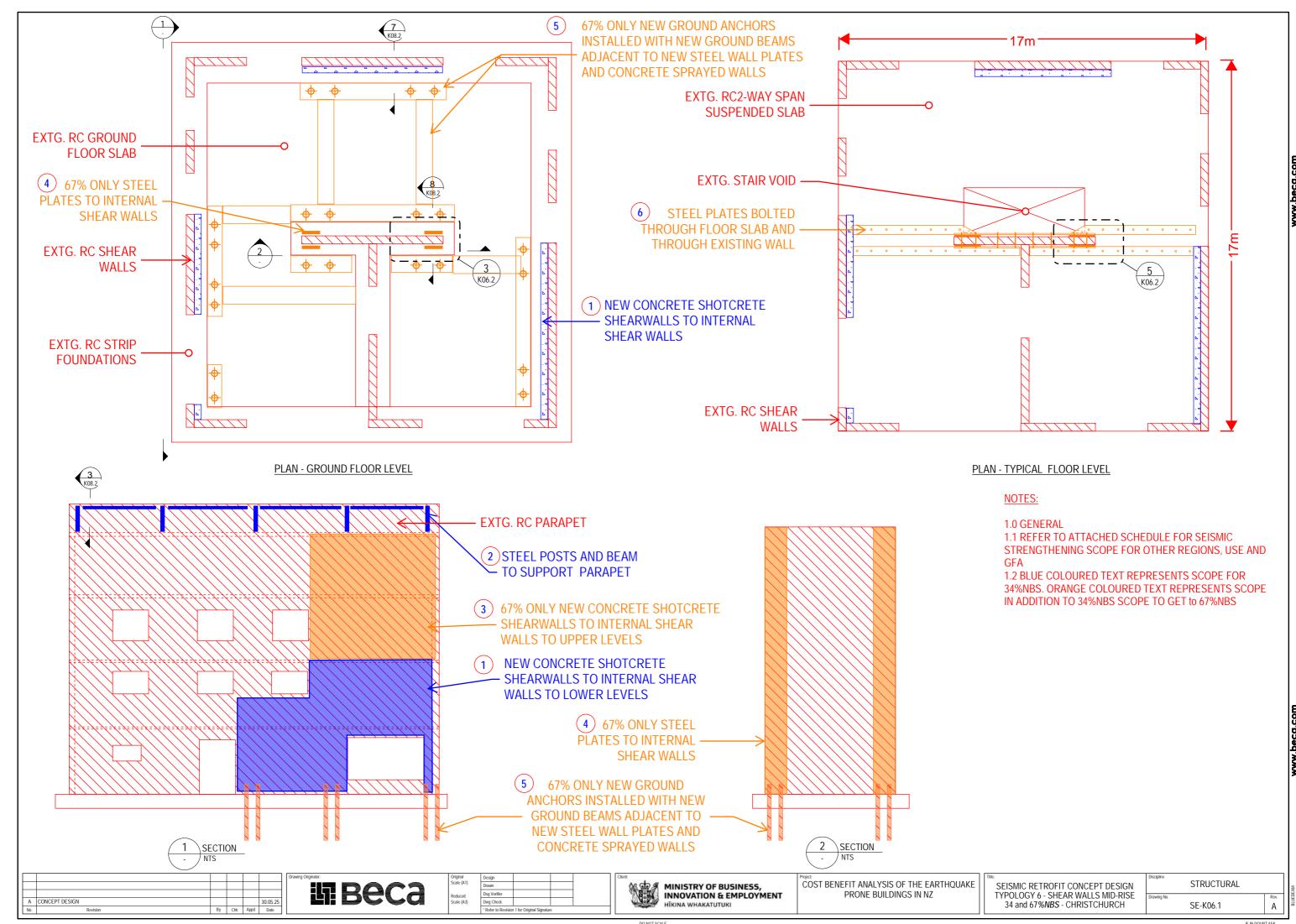
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Scale (A1)	Drawn		
Reduced Scale (A3)	Dsg Verifier		
	Dwg Check		









0

DIAPHRAGM DRAG TIE K06.1

STRENGTHENING

NEW STEEL PLATES FIXED TO SLAB

**WALL PLATE** 

K06.1

STRENGTHENING

EXISTING RC WALL

**EXISTING WALL** 

STEEL PLATES BOLTED TOGETHER THROUGH THE

> NEW RC SHOTCRETE WALL EPOXY FIXED AND LINING EXISTING WALL NEW RC FOUNDATION BELOW NEW WALL WITH GROUND ANCHORS DRILLED INTO EXISTING GROUND **NEW GROUND** BEAM BELOW

**PARAPET** 

**STRENGTHENING** 

K06.1

EXISTING RC SLAB

**NEW WALL INCLUDING** K06.1 **GROUND ANCHORS** 

**SECTION THROUGH TIE** 

**NEW STEEL WALL TIES** INCLUDING GROUND ANCHORS

A CONCEPT DESIGN
No.

**III** Beca

**EXISTING RC** 

PARAPET



**NEW STEEL CONTINUOUS PFC** 

**ROOF SLAB** 

EXISTING RC ROOF

SLAB

NEW STEEL POSTS WITH BACK BRACE FIXED TO THE

PARAPET AND TO THE

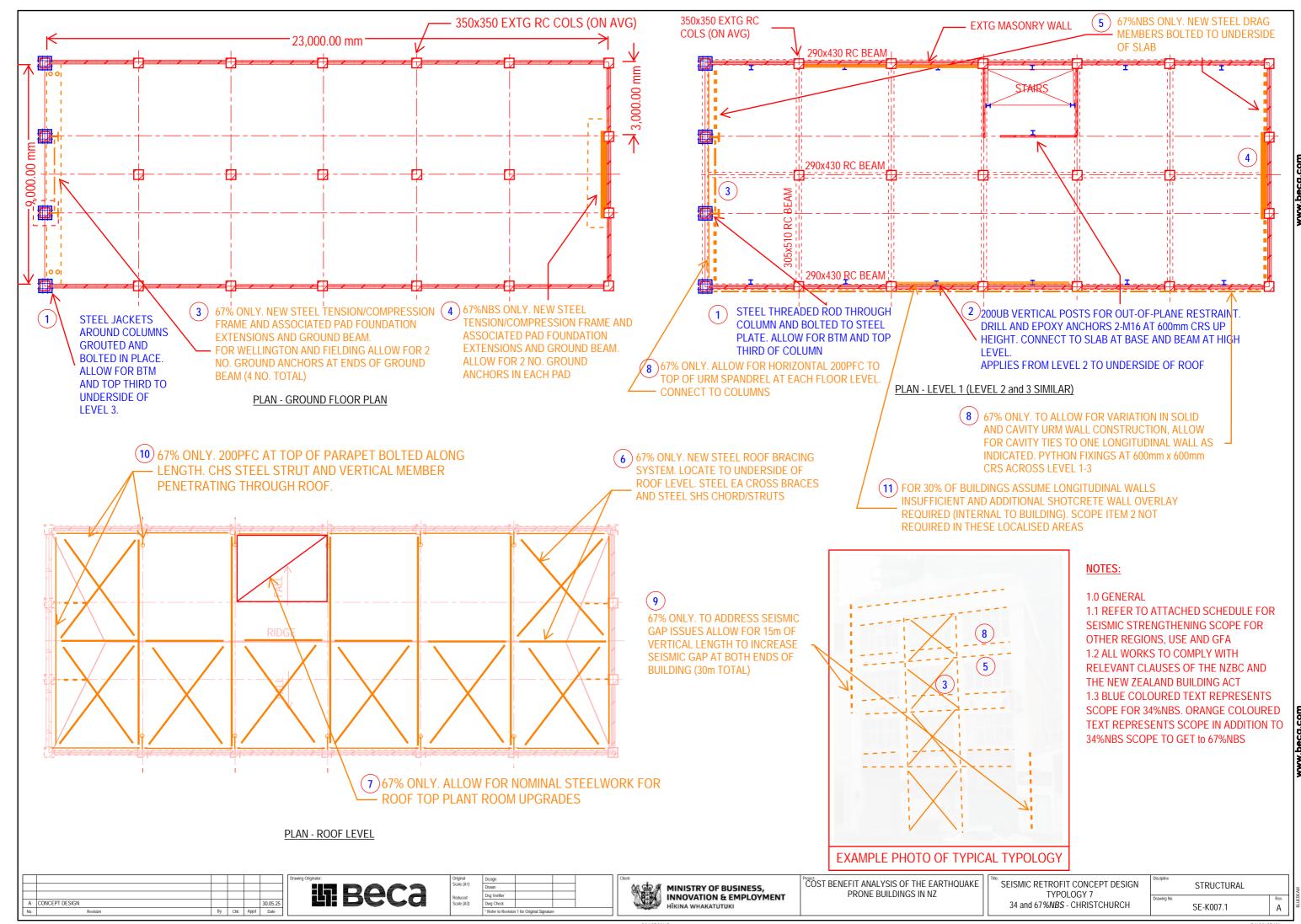
EXISTING RC

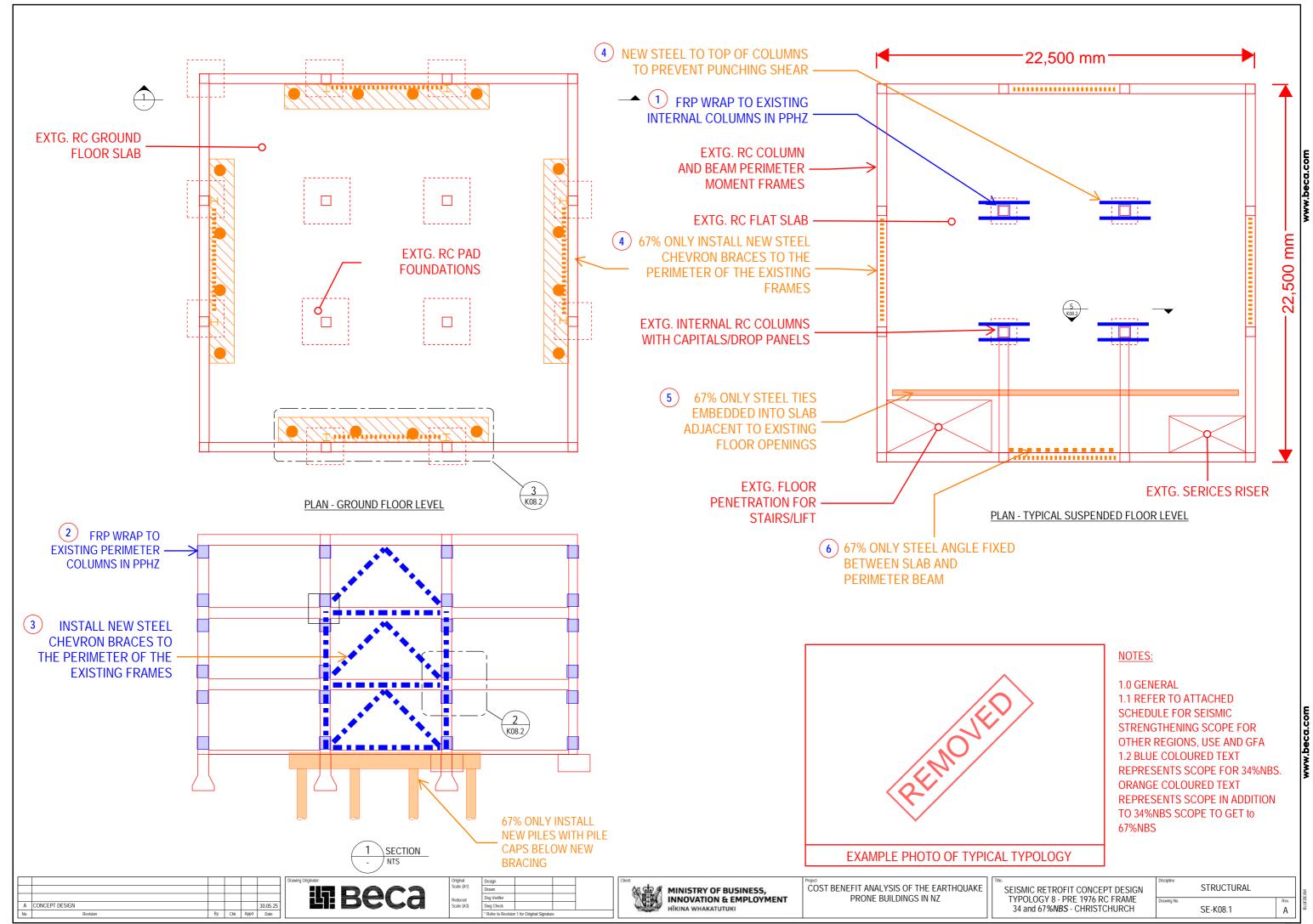
SHEAR WALL

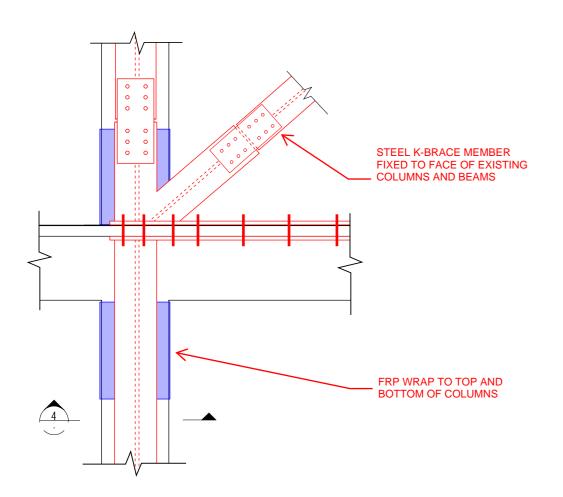
COST BENEFIT ANALYSIS OF THE EARTHQUAKE PRONE BUILDINGS IN NZ

SEISMIC RETROFIT CONCEPT DESIGN TYPOLOGY 6 - SHEAR WALLS MID-RISE 34 and 67%NBS - CHRISTCHURCH

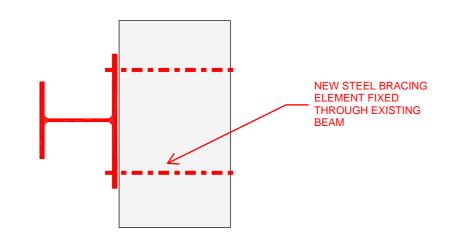
STRUCTURAL SE-K06.2



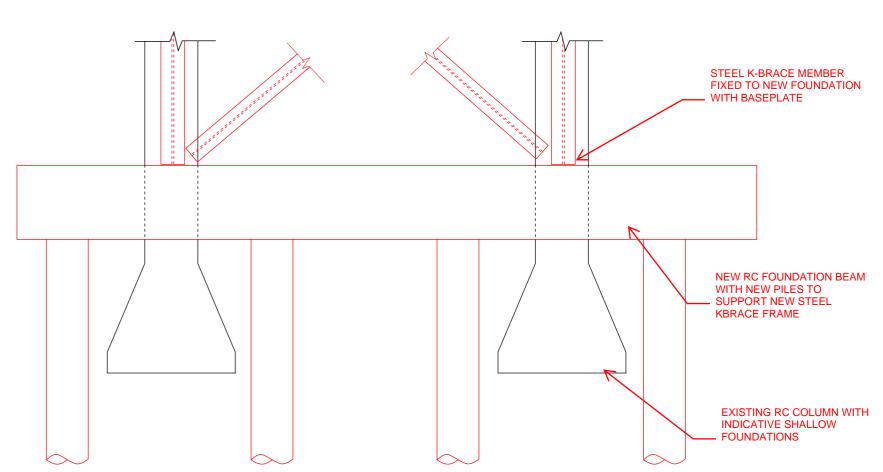




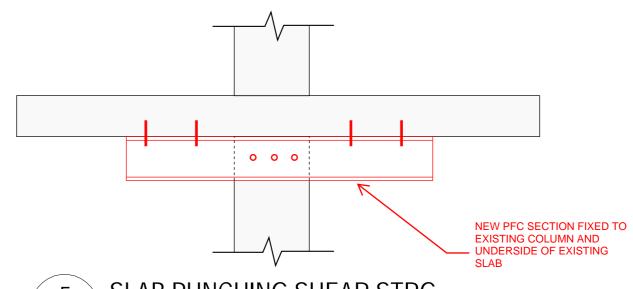




4 SECTION THROUGH KBRACE
- NTS



3 FOUNDATION STRENGTHENING
K08.1 NTS



5 SLAB PUNCHING SHEAR STRG

K08.1 NTS

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Scale (A1) Dosan

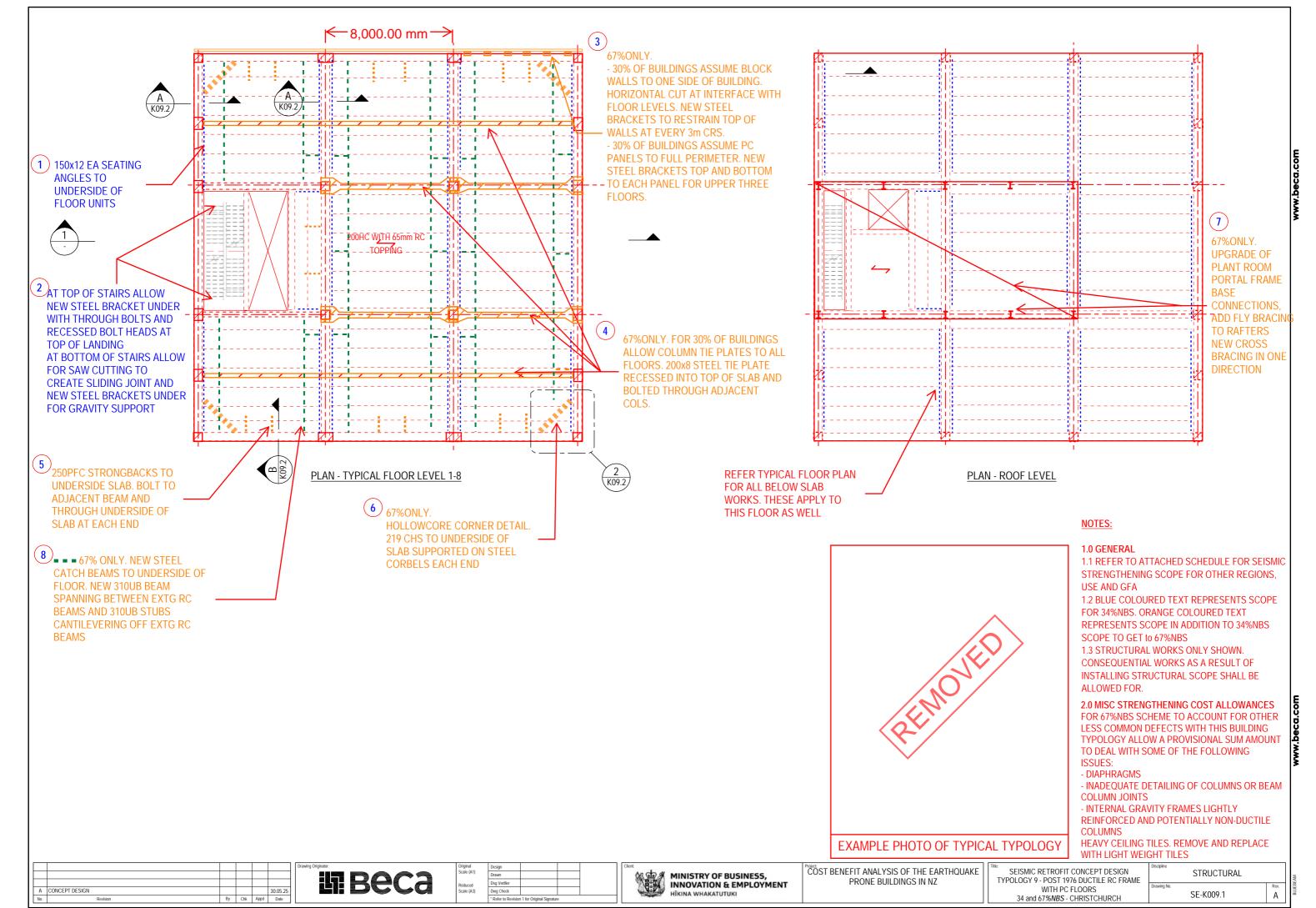
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\* Refer to Revision 1 for Original Signature

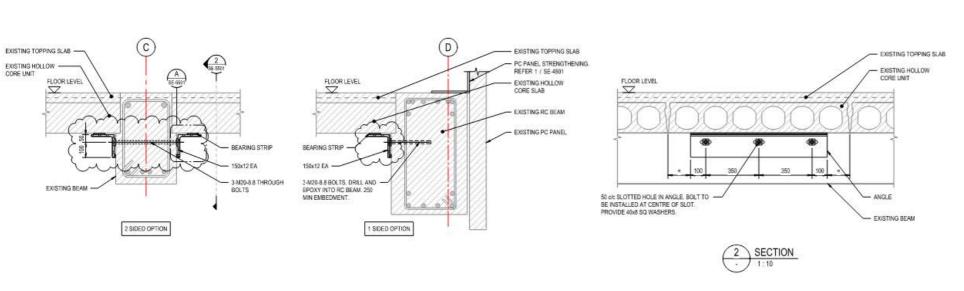


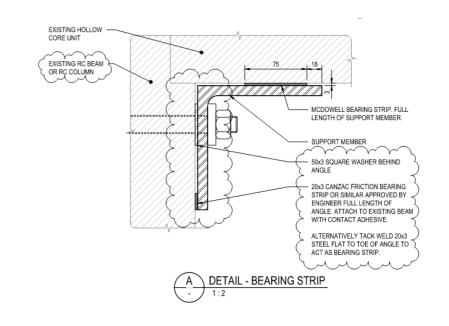
COST BENEFIT ANALYSIS OF THE EARTHQUAKE PRONE BUILDINGS IN NZ

SEISMIC RETROFIT CONCEPT DESIGN TYPOLOGY 8 - PRE 1976 RC FRAME 34 and 67%NBS - CHRISTCHURCH

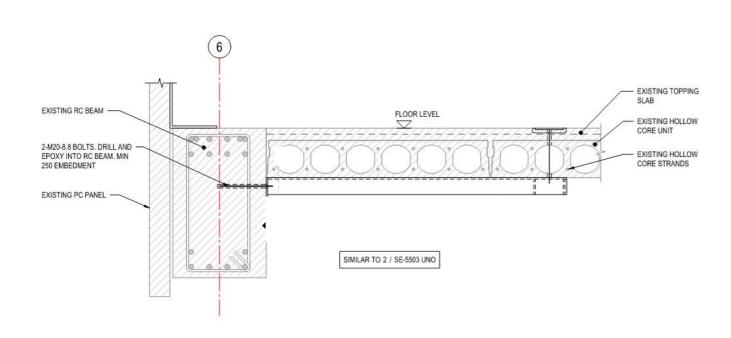
Discipline
STRUCTURAL
Drawing No.
SE-K08.2
Rev.

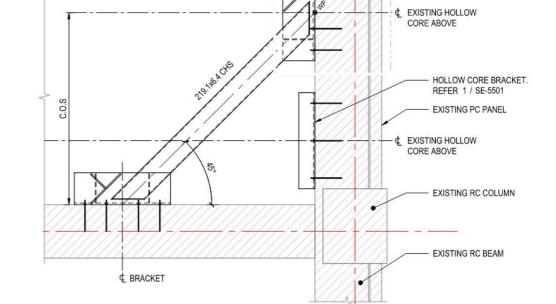






A TYPICAL HOLLOWCORE SEATING DETAIL





B TYPICAL ALPHA SLAB DETAIL K09.1

2 TYPICAL HOLLOWCORE CORNER DETAIL

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ı	No.	Revision	Ву	Chk	Appd	Date

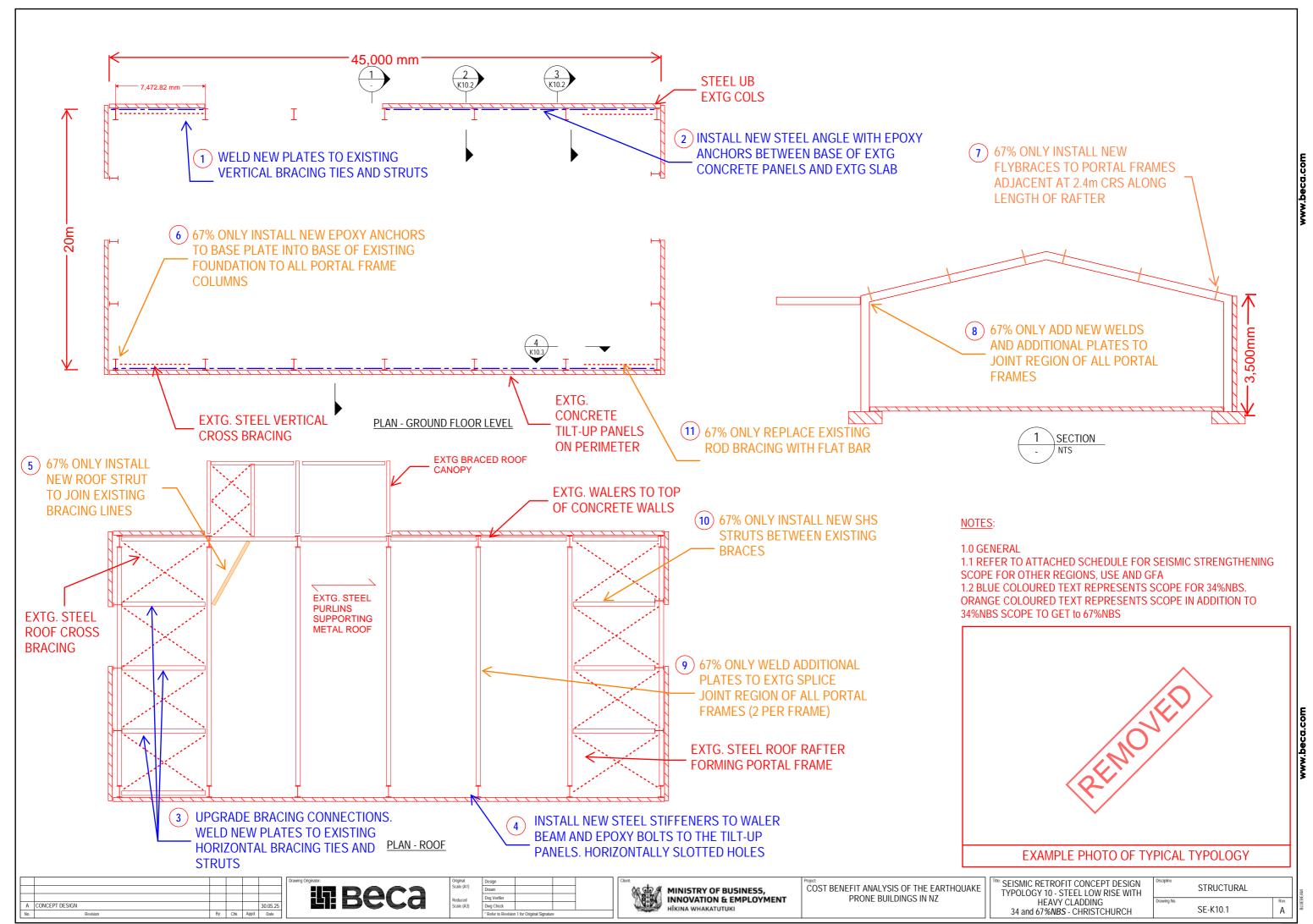
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Reduced	Dsg Verifier									
Scale (A3)	Dwg Check									
	* Refer to Revision 1 for Original Signature									



COST BENEFIT ANALYSIS OF THE EARTHQUAKE PRONE BUILDINGS IN NZ

SEISMIC RETROFIT CONCEPT DESIGN TYPOLOGY 9	Discipline STRUCTURAL				
34 and 67%NBS - CHRISTCHURCH	Drawing No. SE-K009.2	Rev.			













ADD NEW FLYBRACES BETWEEN PURLINS AND PORTAL FRAMES ADJACENT TO COLUMN

ADD NEW FPBW TO EXISTING MOMENT JOINT PLATES AND ADDITIONAL PLATES TO JOINT REGION OF ALL PORTAL FRAMES

INSTALL NEW EPOXY ANCHORS TO BASE PLATE INTO BASE OF EXISTING FOUNDATION TO ALL PORTAL FRAME COLUMNS.

TYPICAL HEAVY CLADDING REMEDIAL

K10.1

(3) K10.1

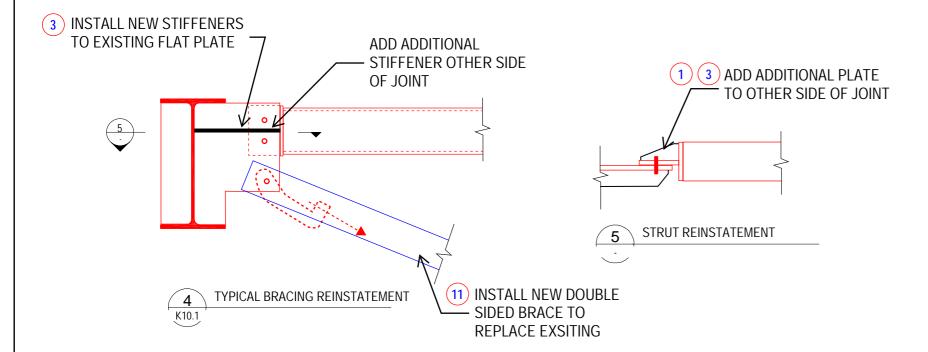
INSTALL NEW STEEL ANGLE WITH EPOXY ANCHORS

BETWEEN BASE OF EXTG

CONCRETE PANELS AND

**EXTG SLAB** 

TYPICAL COLUMN REINSTATEMENT



Α	CONCEPT DESIGN				30.05.25
No.	Revision	By	Chk	Appd	Date

**III** Beca



Project: COST BENEFIT ANALYSIS OF THE EARTHQUAKE PRONE BUILDINGS IN NZ

SEISMIC RETROFIT CONCEPT DESIGN TYPOLOGY 10 - STEEL LOW RISE WITH HEAVY CLADDING 34 and 67%NBS - CHRISTCHURCH

STRUCTURAL SE-K10.2



Appendix E

## Summary of Cost Estimates For Seismic Retrofits



#### 1 Cost Estimation Summary

#### 1.1 Overview

Beca Cost Management have undertaken a feasibility study estimation exercise of scenario based indicative repair strategies for 10 generalised building typologies to achieve both 34% NBS and 67% NBS. These estimates have been subjected to cost modelling to determine aggregated fit out and building services costs, regional market differentiation and building occupancy/functional requirements i.e. *Commercial use building located in Wellington*. Risk contingency, fees and client consenting cost have been included as part of the cost model.

The change in regional seismic requirements (Z values) have been captured by the Beca Structural Team and were provided to Beca Cost Management within the **Strengthening Schedules 1-10**. These are represented in the Schedules as percentages of scope for each construction element with Christchurch set as a baseline of 100%.

Energy efficiency was included in the scope at a later date and is limited in its application to areas only impacted by construction activity. Allowances for fire upgrades have been quantified for 67% NBS options only.

#### Regions Included:

- Christchurch (base estimate)
- Dunedin
- Auckland
- Whanganui
- Feilding
- Wellington

#### **Building Functions:**

- Residential
- Commercial
- Industrial
- Hospitals (limited)

Please find attached a summary table of cost per m<sup>2</sup> in Appendix A.

#### 1.2 Basis of Estimate

The estimate has been based on structural design information provided by Beca Structural Engineers.

These are high level single point estimates with each estimate being conducted using Christchurch market conditions and rates as a baseline. These estimates have been put through cost modelling to determine indicative cost for the other regions included in this study.

Design information provided by Beca Structural:

- Preliminary Sketches
  - Typology 1: 34% & 67% NBS SE-K001.1, SE-K001.2
  - Typology 2: 34% & 67% NBS SE-K002.1, SE-K002.2
  - o Typology 3: 34% & 67% NBS SE-K003.1, SE-K003.2
  - Typology 4: 34% & 67% NBS SE-K004.1, SE-K004.2, SE-K004.3
  - Typology 5: 34% & 67% NBS SE-K005.1, SE-K005.2
  - Typology 6: 34% & 67% NBS SE-K006.1, SE-K006.2
  - o Typology 7: 34% & 67% NBS SE-K007.1
  - Typology 8: 34% & 67% NBS SE-K008.1, SE-K008.2
  - o **Typology 9**: 34% & 67% NBS SE-K009.1, SE-K009.2
  - Typology 10: 34% & 67% NBS SE-K0010.1, SE-K0010.2
  - Strengthening Schedule: Typ 1, 2, 3, 4 & 10 (Z values)
  - o **Strengthening Schedule**: Typ 5, 6, 7, 8 & 9 (Z values)
  - Tender returned data from regional projects held by Beca
  - Various Market Indices, Including: RLB Indices, QV Indices, Beca Cost Management Market Indices

The costs are in NZD and exclude GST

The base estimation rates used in these estimates are based upon tender returned rates from Christchurch in Q4 2024

#### 1.3 Project on costs

Due to the unique construction conditions for each region covered in this Cost Benefit Analysis Preliminaries and General allowances have been calculated independently for each of the regions and are included in the cost model summary for each typology. The Preliminary and General allowance is based on an average of market returned data for each region at the time of this analysis.

Market conditions and contractor availability are unique to each region and subject to fluctuations for this reason Contractor Margin has been calculated independently for each of the regions and is included in the cost model summary for each typology. This Margin is based on an average of market returned data for each region at the time of this analysis.

#### 1.4 Assumptions

These general assumptions are applicable to all building typologies, regions and seismicity scope (34% NBS & 67% NBS):

- · Assumed that buildings will be unoccupied for the duration of the construction activity
- All floor areas and building layouts are indicative and actual buildings will be subject to unique requirements not represented in this exercise
- All pricing is based on drawings provided by the engineers and does not make allowance for specialist areas unduly impacted by Construction activity i.e. Commercial kitchens, Laboratories. Server rooms etc.
- · Assumed all works would be undertaken in a single phase
- Assumed work would be undertaken during normal working hours (7:30am 5:00pm Monday Friday)
- The base rate has been calculated based upon Christchurch Q4 2024 cost data, derived from average tender pricing for each of the itemised structural scope requirements as defined within the structural drawing details
- The costs values within the summary for each typology are provided as an indicative guide for the scope of seismic improvement works for each typology.
- No allowance has been made for upgrades or replacement of any fit-out fittings or fixtures or improvements to building services. The allowances are only for removal and reinstatement
- Assumed that reasonable site access is available
- The Energy Efficiency costs supplied as part of these cost estimates are only relative to the
  areas impacted by structural scope. And no allowances have been made to uplift adjoining
  areas or services improvements relating to energy efficiency.
- Energy Efficiency upgrades are limited to increased wall and roofing insulation along with window joinery (glazing included) to areas directly impacted by structural scope.
- Fire Compliance upgrades were only considered to be triggered with larger seismic upgrade strategies (67% NBS)

#### 1.5 Exclusions

Unless specifically stated otherwise the following items are excluded from the estimated reinstatement costs:

- Goods and services tax (GST)
- Construction escalation beyond date of estimate
- Legal/accounting fees
- Client direct costs
- Costs associated with temporary decanting / relocation of existing building occupancy
- Fast track or accelerated programme
- Work outside normal hours
- · Incurred costs to date
- No allowance made for testing, excavation, removal and disposal of contaminated materials
- Temporary protection / security as external wall opened
- Traffic Management
- Staging / phased work
- Insurances
- Site security
- Signage

- Geotechnical risk The cost of additional depths of foundation pads and ground beams required by ground conditions – ranging from deeper foundations to gravel rafts or piled systems.
- No allowance for building improvements all costs are based on replacing finishes with similar. appropriate linings and surface coverings.
- No allowance has been made for building services upgrades.
- No allowance for hard landscaping paths and access more than 1m from the face of the building.
- No allowance for landscaping and maintenance works.

#### 1.6 Disclaimers

This report is solely for our client's use for the purpose for which it is intended in accordance with the agreed scope of work. It may not be disclosed to any person other than the Client and any use or reliance by any person contrary to the above, to which Beca has not given its prior written consent is at that person's own risk.

This report must be read in its entirety and no portion of it should be relied on without regard to the report as a whole, especially the assumptions, limitations and disclaimers set out in the estimate notes and elsewhere in the report.

While Beca believes that the use of the assumptions in the report are reasonable for the purposes of this study, Beca makes no assurances with respect to the accuracy of such assumptions, and some may vary significantly due to unforeseen events and circumstances.

In preparing this estimate, Beca has relied on the accuracy, completeness and currency of the information provided, therefore is not responsible for the information provided, and has not sought to independently verify it. To the extent that the information is inaccurate or incomplete, the opinions expressed by Beca may no longer be valid and should be reviewed.



Appendix A – Cost Per M<sup>2</sup> Summary

#### MBIE Seismically Prone Buildings - Cost Benefit Analysis - Cost Per M<sup>2</sup> Summary

Typology		Тур - 1		Typ - 2		Тур - 3		Typ - 4		Typ - 5		Typ - 6		Тур - 7	Typ - 8		Typ - 9		Typ - 10				
Building function			Comm	Res	Comm	Res	Comm	Res	Comm	Res	Ind	Comm	Res	Comm	Res	Ind	Comm	Comm	Res	Comm	Res	Comm	Ind
Christchurch																							
GFA			20		200		500		4320		336	300	1156		830	1500		5400		900			
	34% NBS	\$/m²	\$ 39.00				\$2,044.00								\$1,218.00					\$1,544.00			
	67% NBS		\$1,228.00	\$ 982.00	\$3,801.00	\$3,331.00	\$4,198.00	\$3,743.00	\$4,785.00	\$4,329.00	\$3,526.00	\$4,832.00	\$4,717.00	\$2,994.00	\$2,538.00	\$1,735.00	\$5,359.00	\$4,728.00	\$4,272.00	\$3,490.00	\$3,035.00	\$2,541.00	\$1,282.00
Auckland	Į.																						
	GFA	200		200		500		4320		336		1156		830	1500		5400		900				
	34% NBS	\$/m²	\$ 40.00				\$1,810.00													\$1,499.00			
	67% NBS		\$ 968.00	\$ 711.00	\$2,569.00	\$2,079.00	\$3,213.00	\$2,739.00	\$3,688.00	\$3,213.00	\$2,378.00	\$3,727.00	\$3,451.00	\$3,069.00	\$2,594.00	\$1,759.00	\$4,667.00	\$4,906.00	\$4,432.00	\$3,528.00	\$3,054.00	\$2,450.00	\$1,140.00
Dunedin	Ļ																						
	GFA		200		200		500		4320		336		1156		830	1500		5400		900			
	34% NBS	\$/m²	\$ 40.00				\$1,796.00													\$1,487.00			
	67% NBS	Ţ	\$ 960.00	\$ 706.00	\$2,472.00	\$1,987.00	\$3,188.00	\$2,717.00	\$3,658.00	\$3,188.00	\$2,359.00	\$3,698.00	\$3,423.00	\$3,044.00	\$2,574.00	\$1,745.00	\$4,631.00	\$4,867.00	\$4,397.00	\$3,501.00	\$3,030.00	\$2,431.00	\$1,131.00
Whanganui	Ļ																						
	GFA		200		200		500		4320		336		1156		830	1500		5400		900			
	34% NBS	\$/m²	\$ 39.00						\$2,252.00							_		\$2,229.00				\$1,340.00	\$ 610.00
	67% NBS		\$1,131.00	\$ 882.00	\$3,310.00	\$2,834.00	\$3,972.00	\$3,511.00	\$4,399.00	\$3,938.00	\$3,126.00	\$4,541.00	\$4,383.00	\$2,982.00	\$2,521.00	\$1,709.00	\$5,051.00	\$4,772.00	\$4,311.00	\$3,499.00	\$3,038.00	\$2,577.00	\$1,304.00
Fielding	Į.																						
	GFA		200 200				00	4320		336		1156		830	1500		5400		900				
	34% NBS	\$/m²	\$ 643.00						\$2,620.00						\$1,232.00			\$2,229.00				\$1,340.00	\$ 610.00
	67% NBS		\$1,328.00	\$1,078.00	\$4,362.00	\$3,886.00	\$4,631.00	\$4,170.00	\$5,040.00	\$4,580.00	\$3,767.00	\$5,368.00	\$5,309.00	\$3,027.00	\$2,566.00	\$1,754.00	\$5,605.00	\$4,780.00	\$4,319.00	\$3,569.00	\$3,108.00	\$2,656.00	\$1,383.00
Wellington	Į.																						
	GFA		200		200		500		4320		336		1156		830	1500		5400		900			
	34% NBS		\$ 711.00				\$2,416.00						\$2,903.00				\$2,491.00	\$2,465.00			\$1,335.00	\$1,482.00	-
	67% NBS		\$1,491.00	\$1,215.00	\$4,862.00	\$4,336.00	\$5,222.00	\$4,712.00	\$5,694.00	\$5,185.00	\$4,286.00	\$6,166.00	\$6,128.00	\$3,348.00	\$2,838.00	\$1,940.00	\$6,344.00	\$5,287.00	\$4,777.00	\$3,967.00	\$3,458.00	\$2,937.00	\$1,529.00



### Appendix F

# Fragility Curves – Comparison With HAZUS And CEBA



## Appendix F – Fragility Curves - Comparison with HAZUS and CEBA

The following figures show comparison of DBM fragility curves (this study) for each type versus Hazus and fragility curves based on the CEBA data from Christchurch February 2011 event. The exercise of this was to test and review the derived DBM fragility curves carefully by comparing them with international standards and Christchurch data.

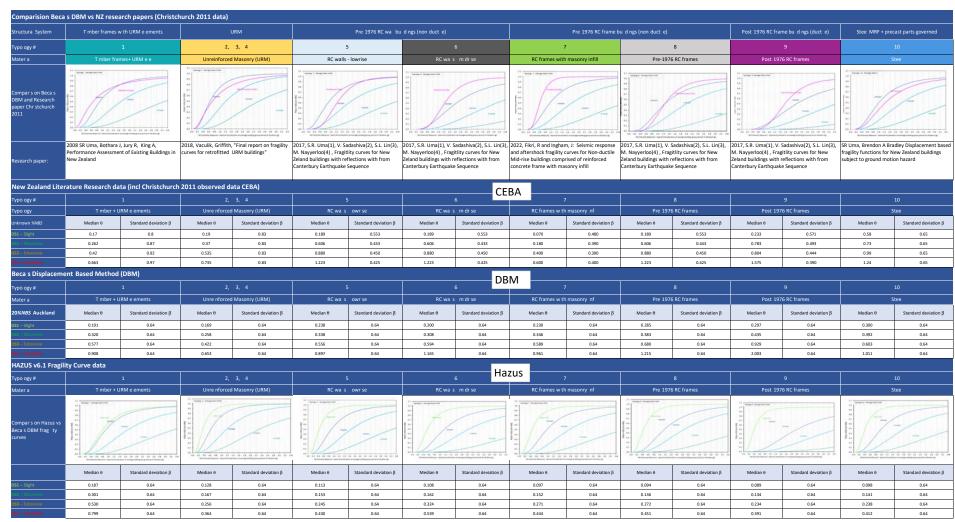
For the Christchurch 2011 data, we used NZ research papers, which already tested and calibrated fragility curves with CEBA actual observed damage data from Christchurch event.

As part of the fragility review, we allocated the building type to the Hazus structural type. Key difference in the comparison of fragility curves is the allocation of the Hazus structural type and spectral displacement associated with each type. The observed differences were attributed to the choice of equivalent Hazus structural types and their associated DS4 spectral displacement capacities. These displacement capacities strongly correlate with the spectral acceleration values observed, confirming that Hazus appropriately reflects the relative collapse capacities of these structural types.

Additionally, the high spectral acceleration values for retrofitted buildings align well with observations from Christchurch, where unstrengthened buildings experienced partial collapses but very few fully collapsed. This supports our calibration, indicating that strengthened structures require higher intensities to reach full collapse. Thus, we believe Hazus is applicable and provides a robust framework for assessing relative building performance in this context.



#### Fragility Curve - Comparsion of Beca's Displ-Based Method (DBM) vs Christchurch 2011 data vs HAZUS data



#### Fragility papers - per Typology

eight structures with or withuout URM elements

1[1] 2008 SR Uma, Bothara J, Jury R, King A, Performance Assessment of Existing Buildings in New Zealand

2 [1] 2018, Vaculik, Griffith, "Final report on fragility curves for retrofitted URM buildings"

2 [2] 2024, Swidan M. I, and Ingham, J.M., Empirical clay brick URM building fragility curves based on the 2011 Christchurch Earthquake 5) + 6) RC wall buildings (low and mid-rise buildings)

5 [1] 2017, S.R. Uma(1), V. Sadashiva(2), S.L. Lin(3), M. Nayyerloo(4), Fragitlity curves for New Zeland buildings with reflections with from Canterbury Earthquake Sequence

5 [2] 2011, June et al - comparision DS vs main shock NZ (fig 4, T=1.3s)
7) RC frames with masonry infill (low and midrise)

7 [1] 2022, Fikri, R; Dizhur, D and Ingham, J: Empirical vulnerability assessment of reinforced concrete frame with masonry infill buildings in the Canterbury earthquake sequence

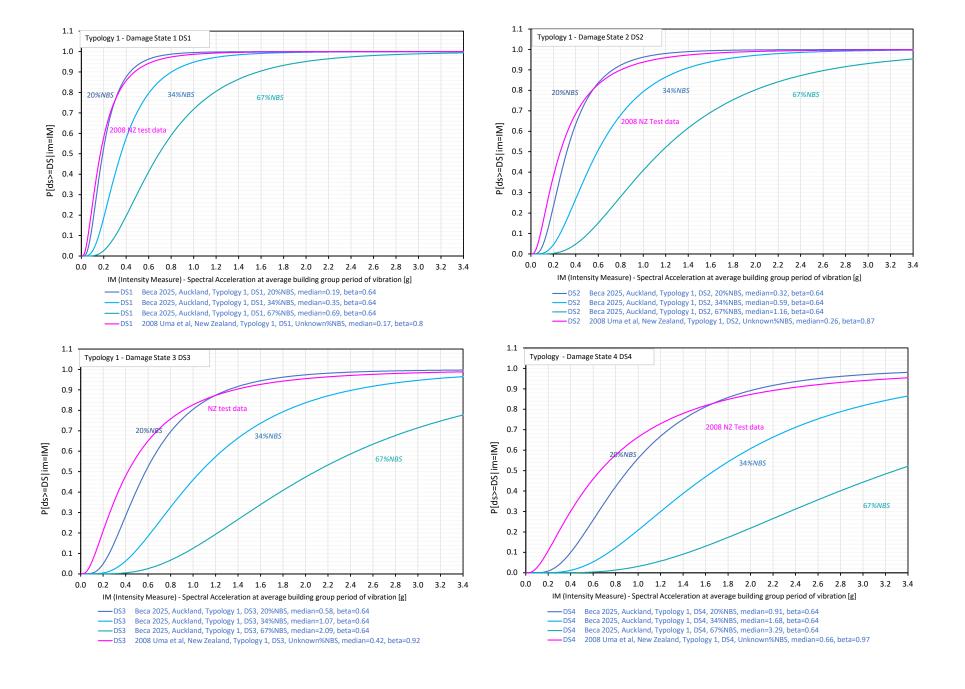
7 [2] 2012, S.R. Uma, H. Ryu, N. Luco, A.B. Liel, M. Raghunandan, Comparison of main-shock and aftershock fingility curves developed for New Zealand and US buildings 7 [3] 2022, F. Rikai, J. Impham: Seismic response and aftershock fingility curves for end-utility mil-first buildings comprises of reinforced converte frames with masonry infill utilities within the Auction replant of Seismic Response and after seasonment for commercial masonry infill utilities within the Auction Reposit Policy Seismic Response and Seismic Response

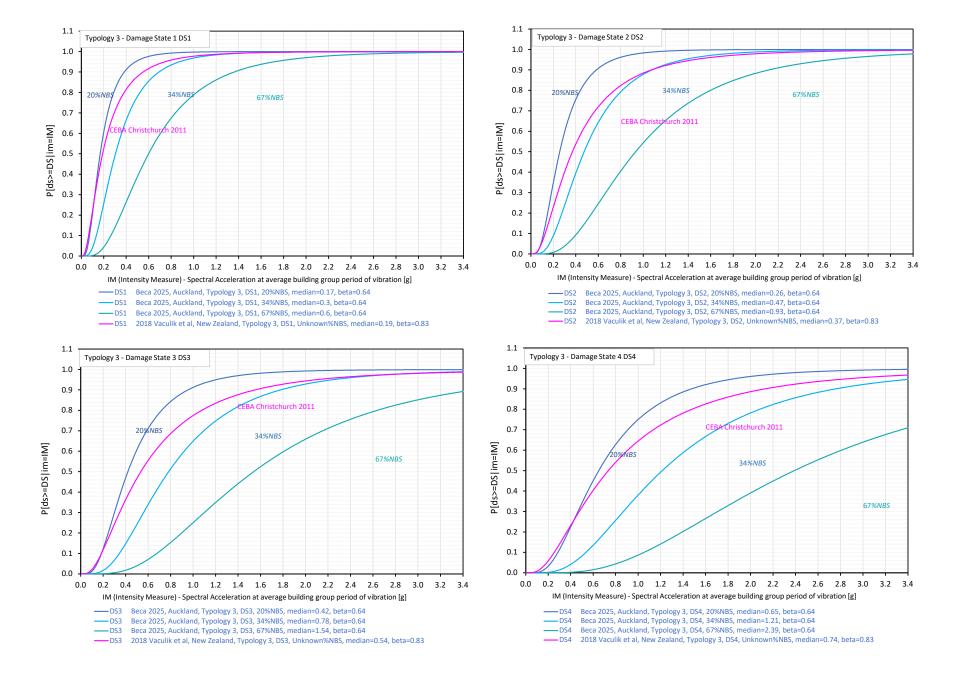
8) Pre-1976 RC frames 

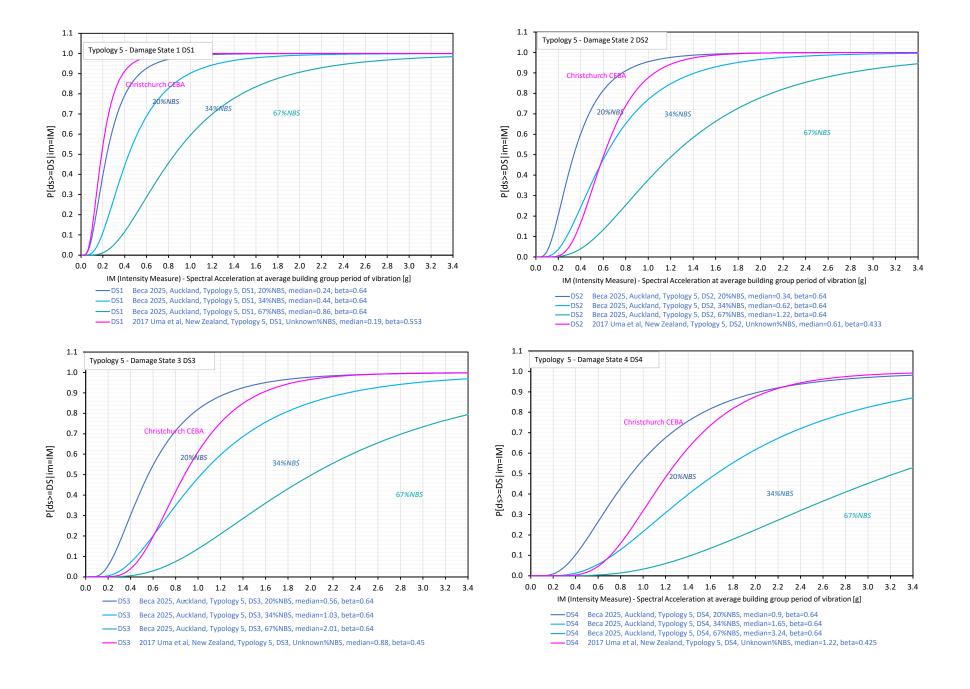
9 [1] 2017. S.R. Uma(1). V. Sadashiya(2). S.L. Lin(3). M. Navyerloo(4). Fragitlity curves for New Zeland buildings with reflections with from Canterbury Earthquake Sequence

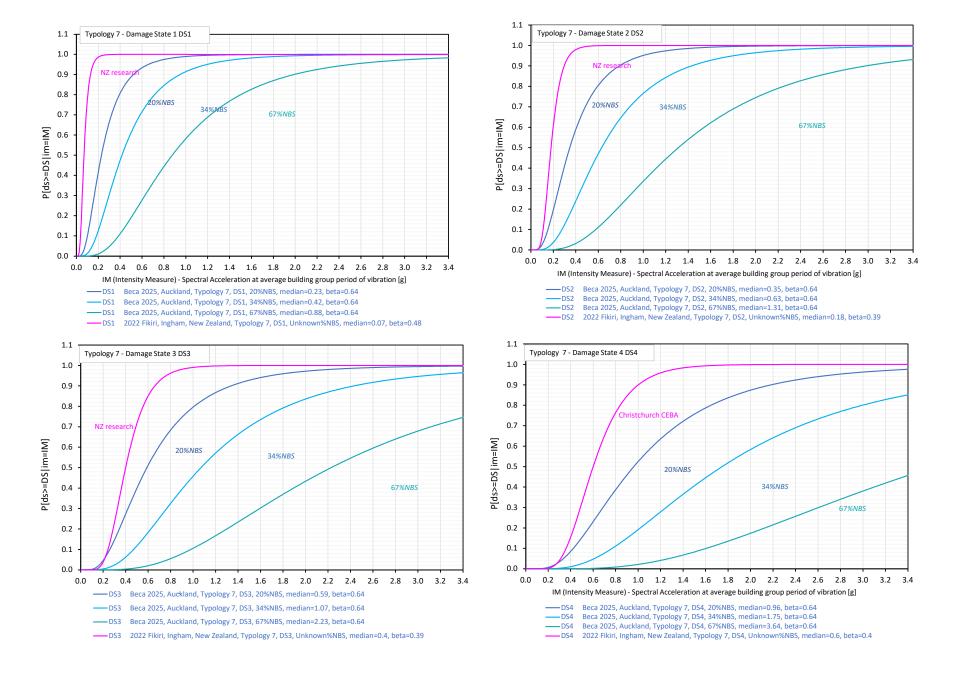
10) Steel MRF buildings
10 [1] SR Uma, Brendon A Bradley Displacement based fragility functions for New Zealand buildings subject to ground motion hazard

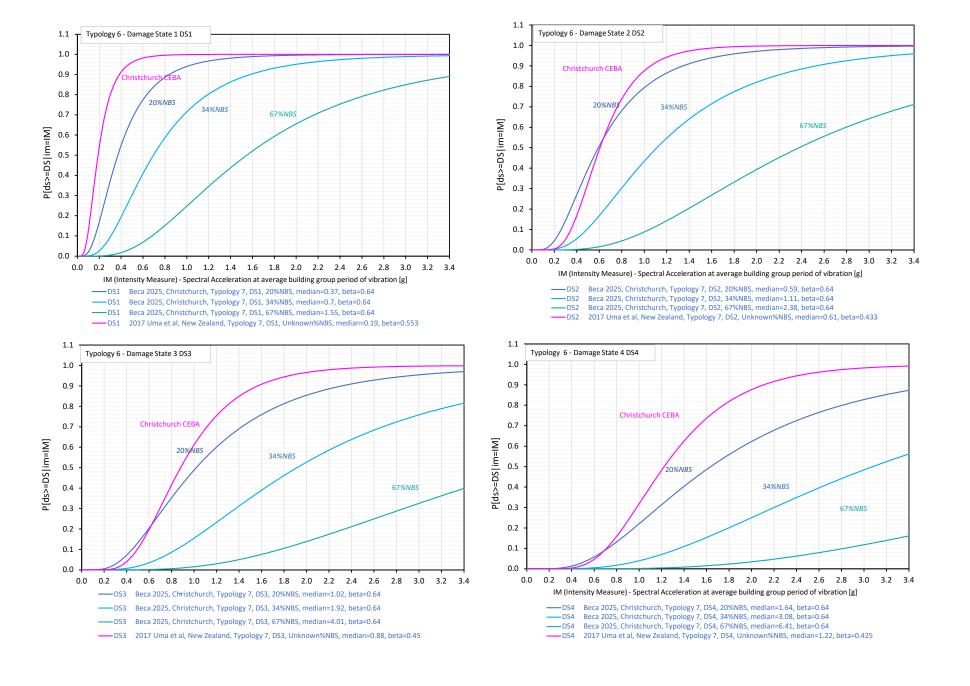
Christchurch 02/2011 (CEBA) comparisons vs DBM fragility curves

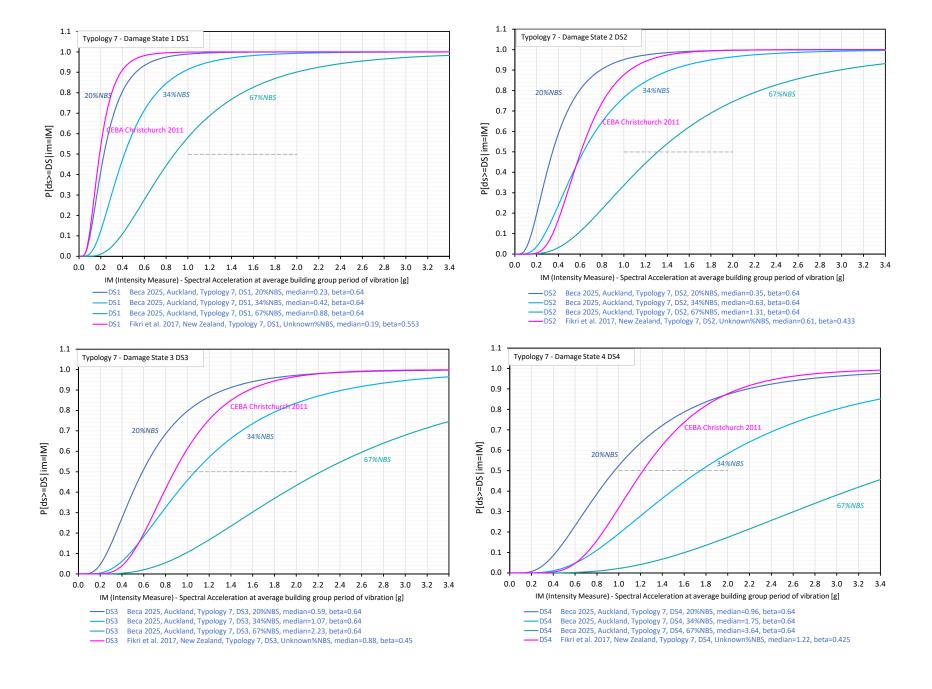


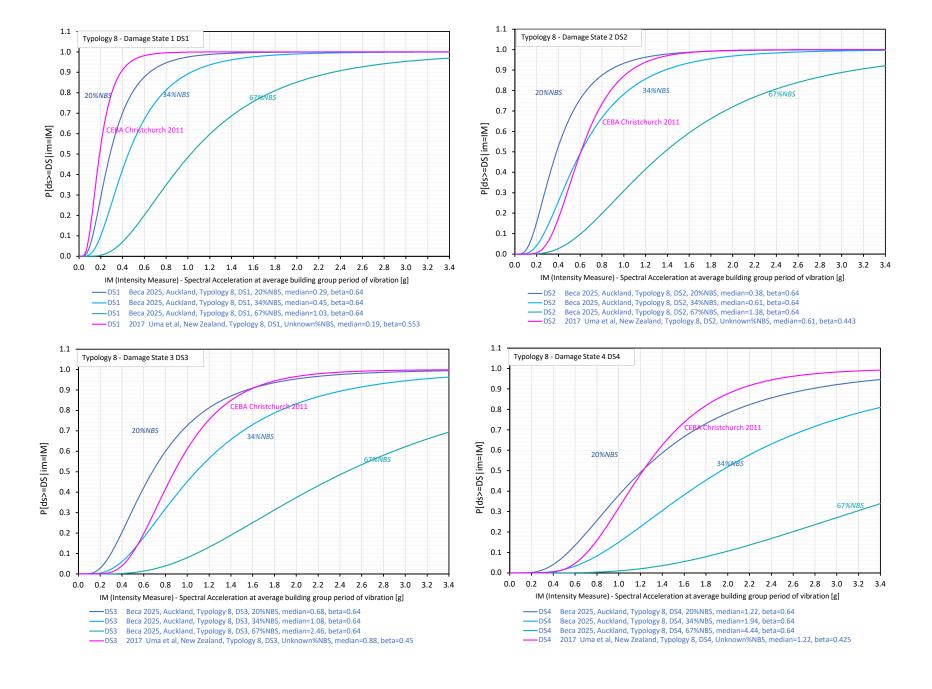


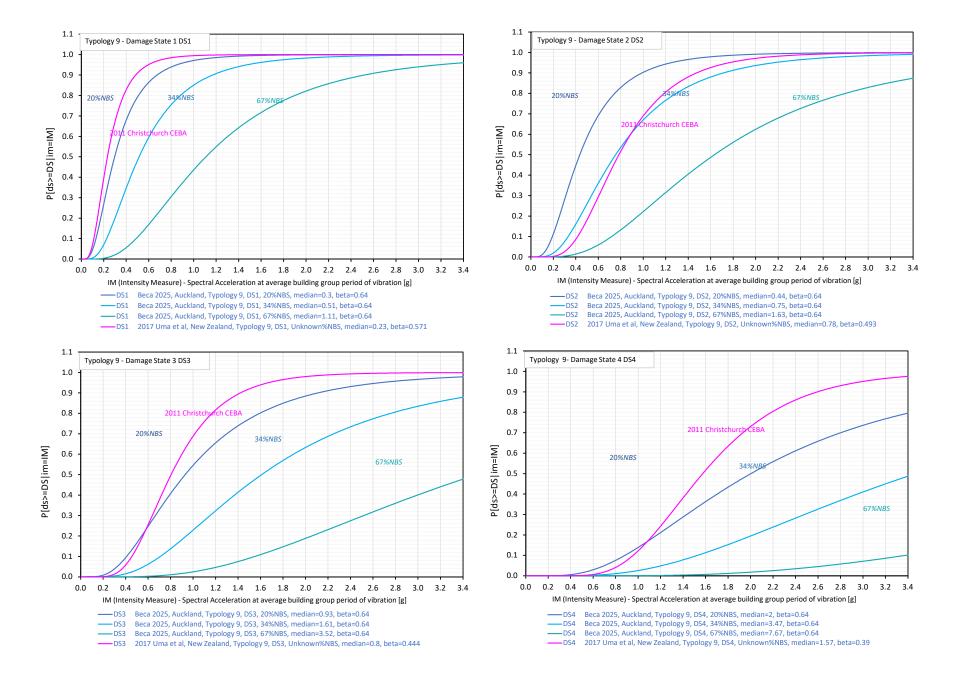


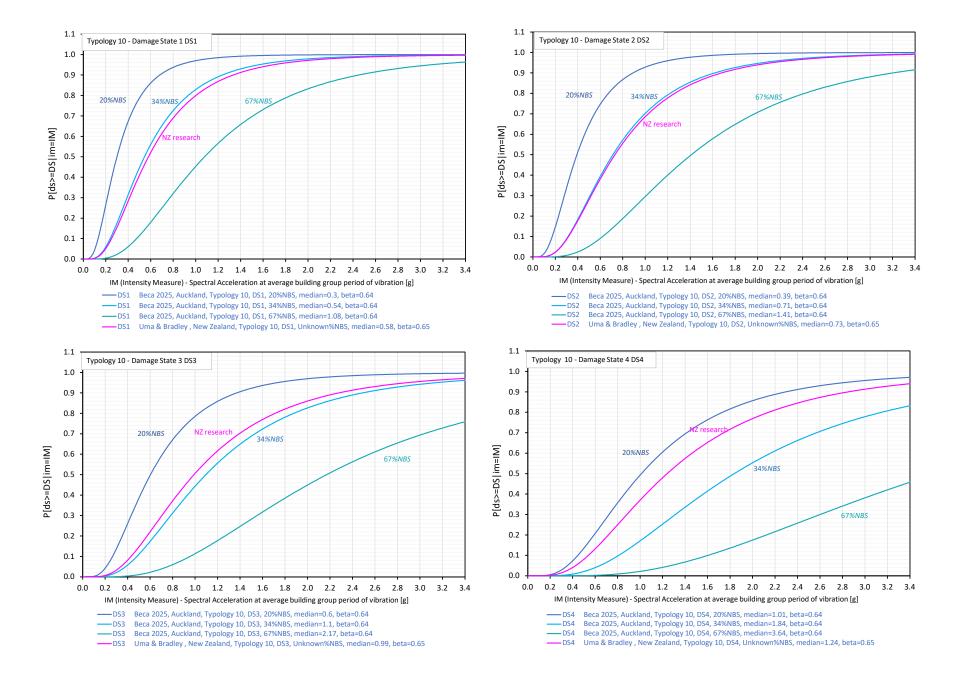


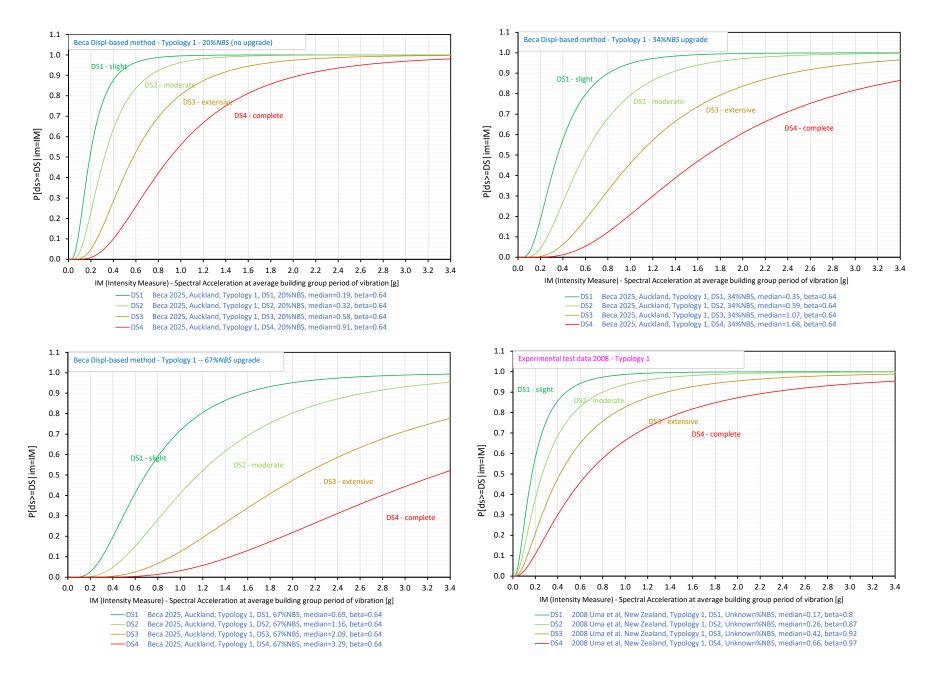


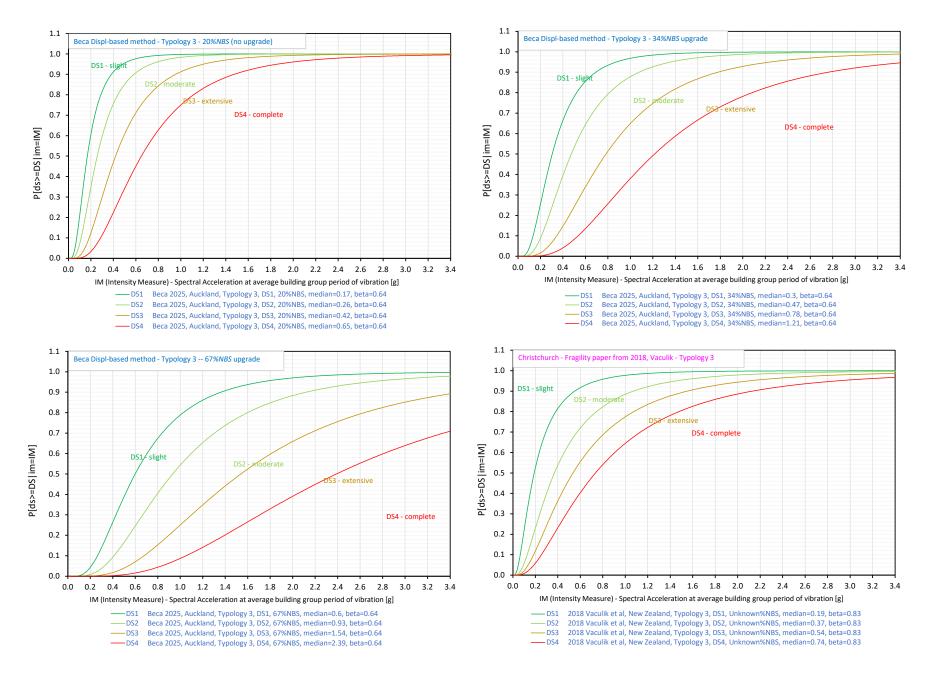


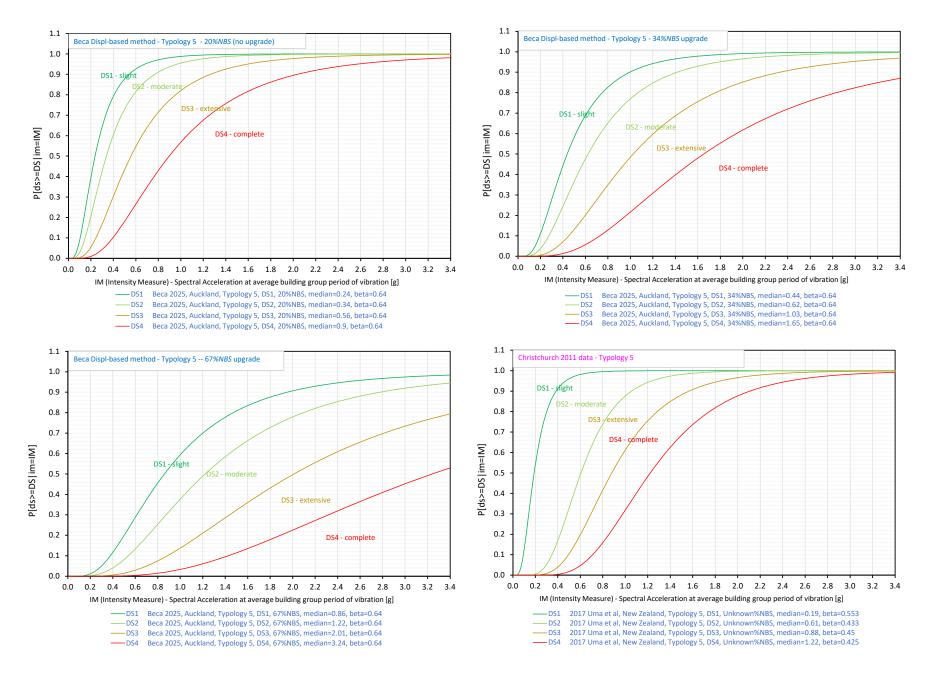


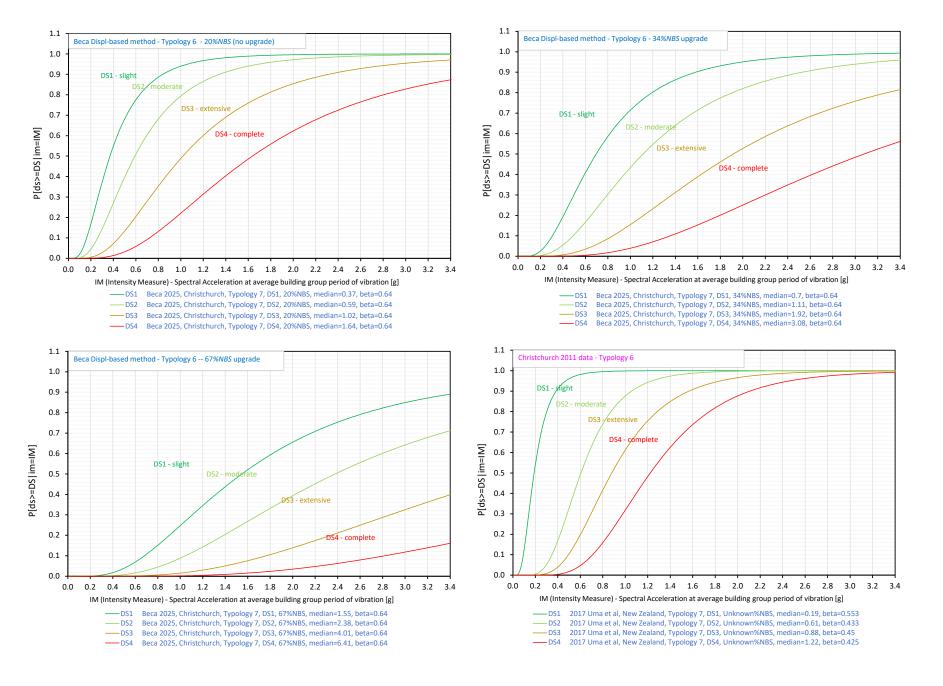


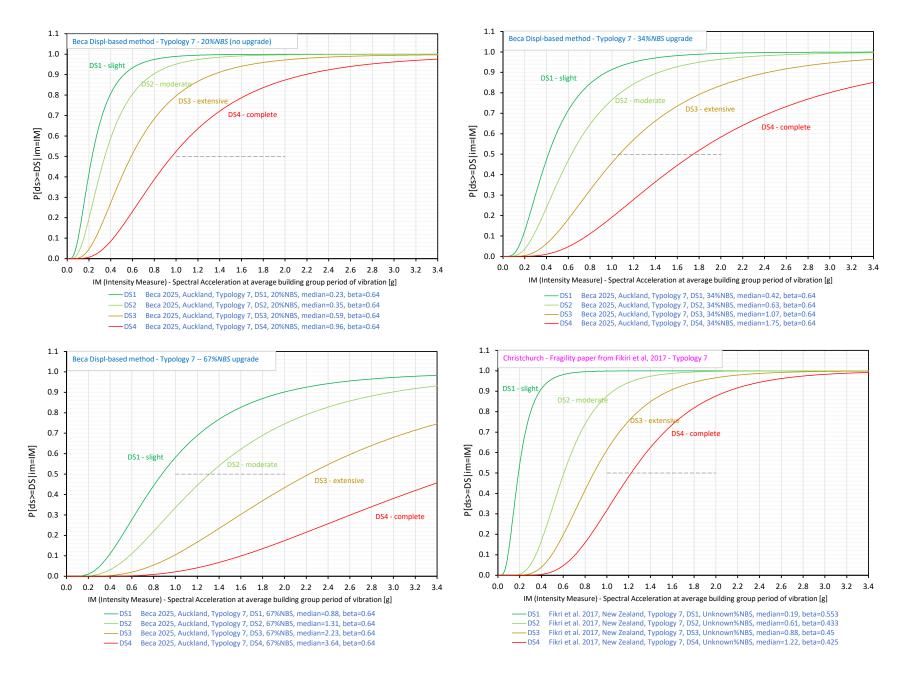


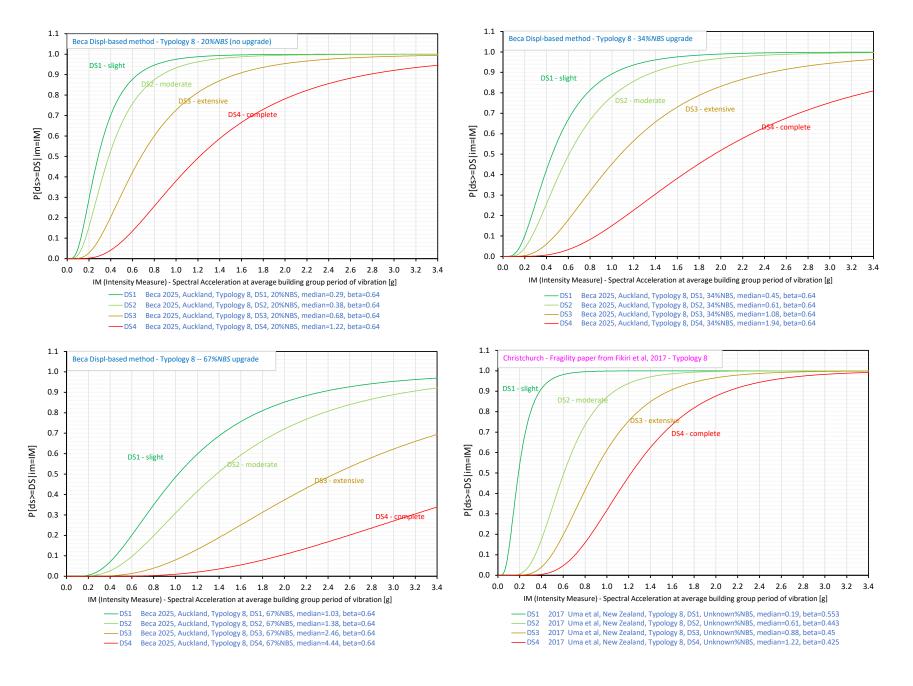


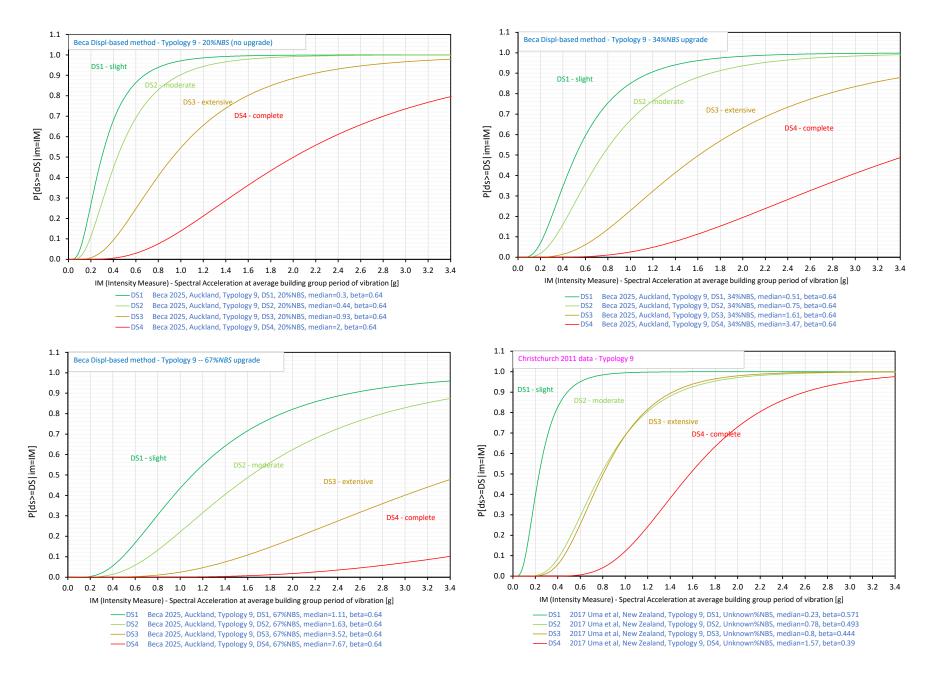


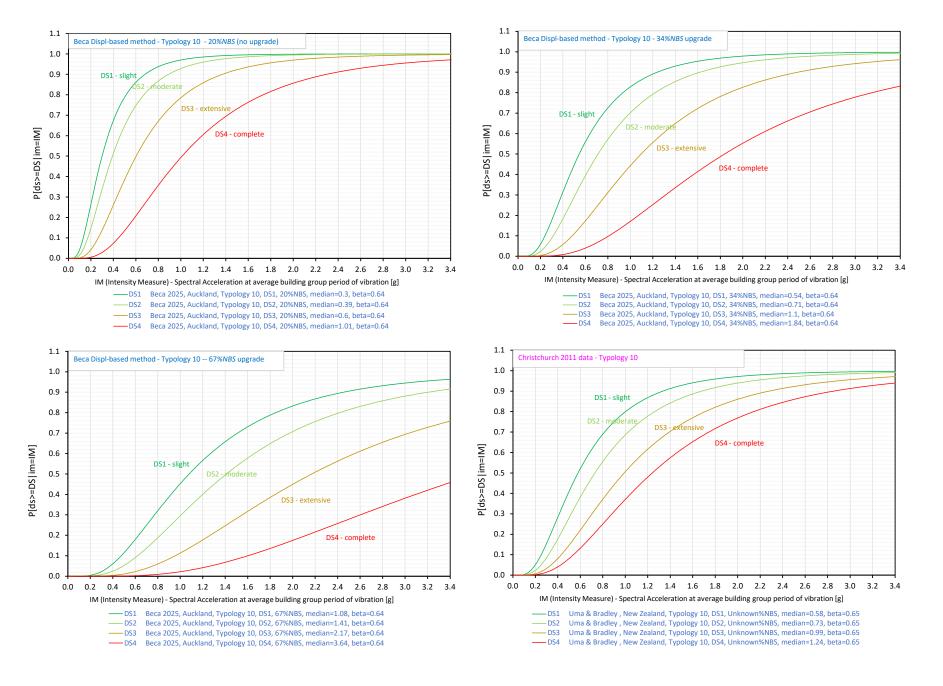




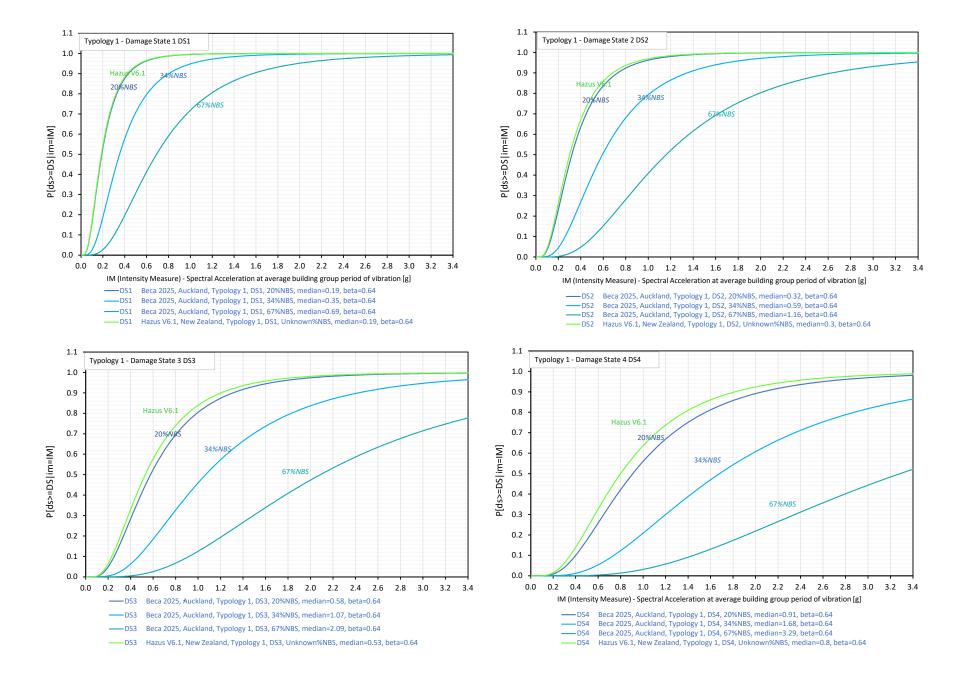


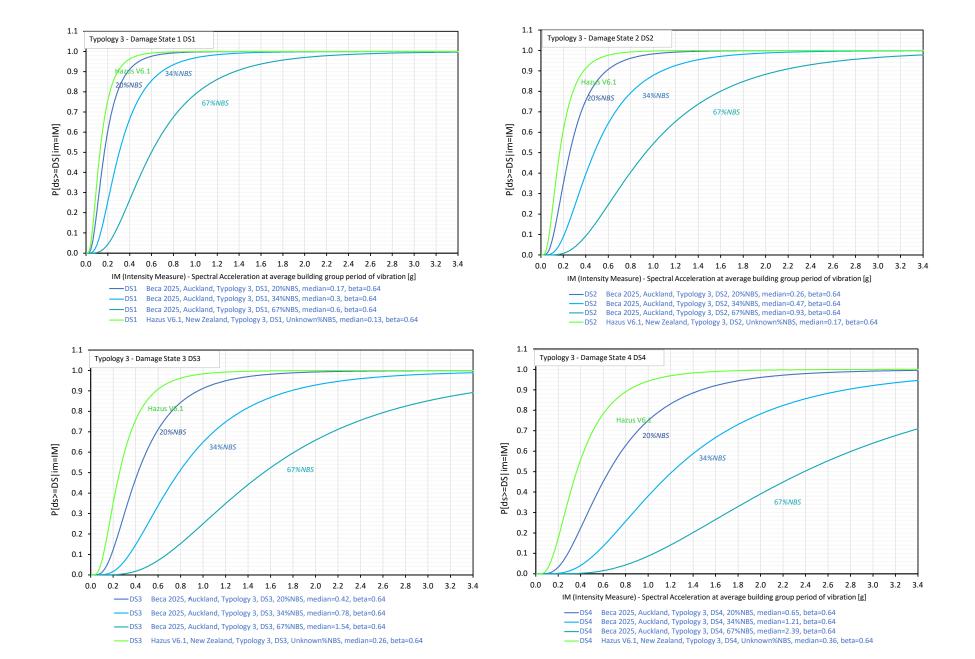


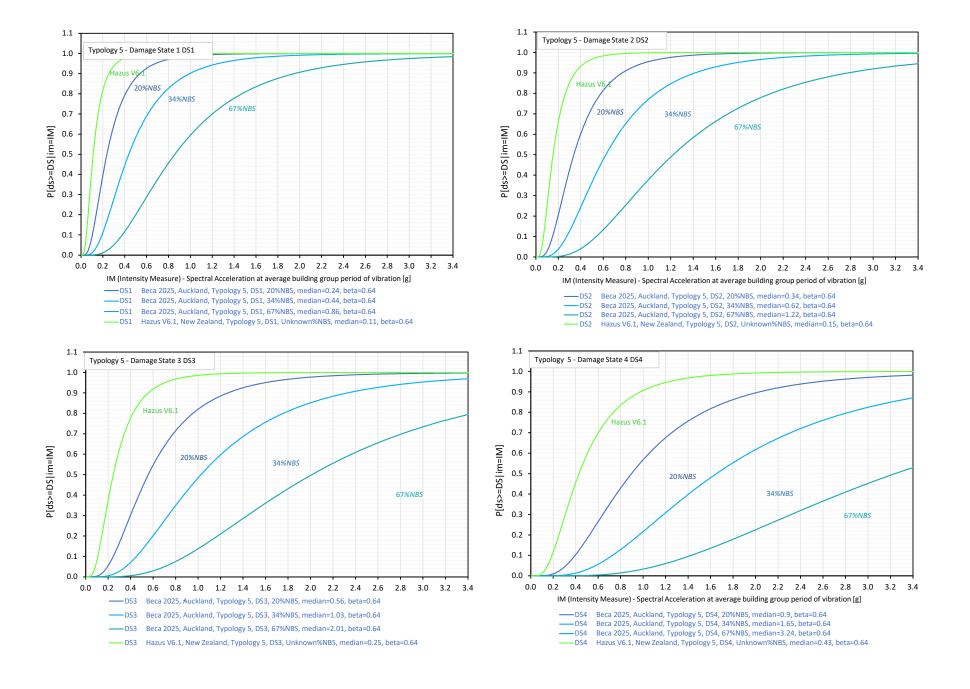


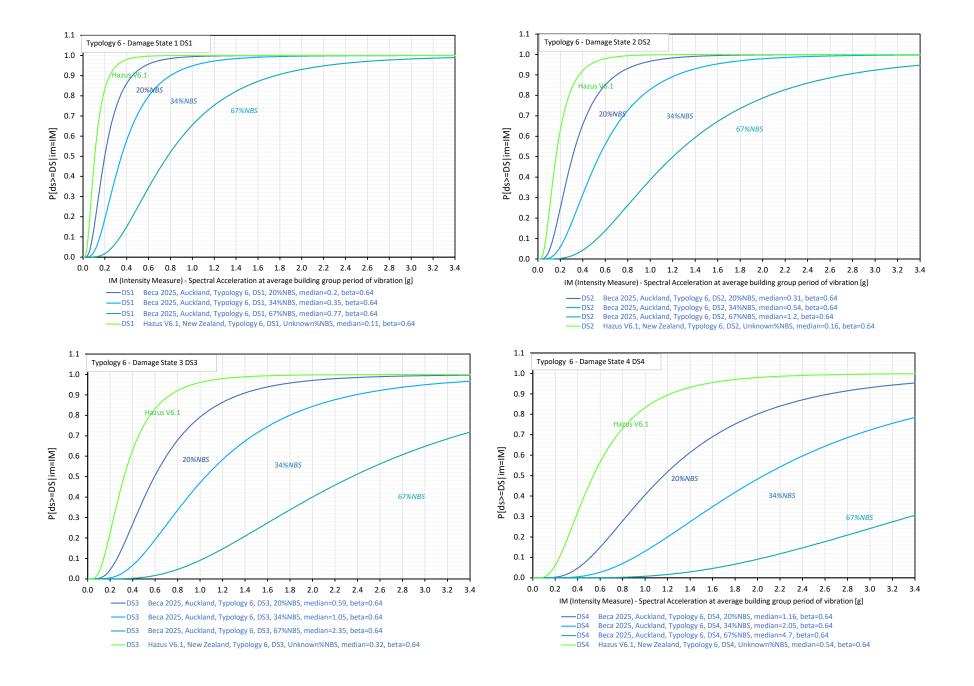


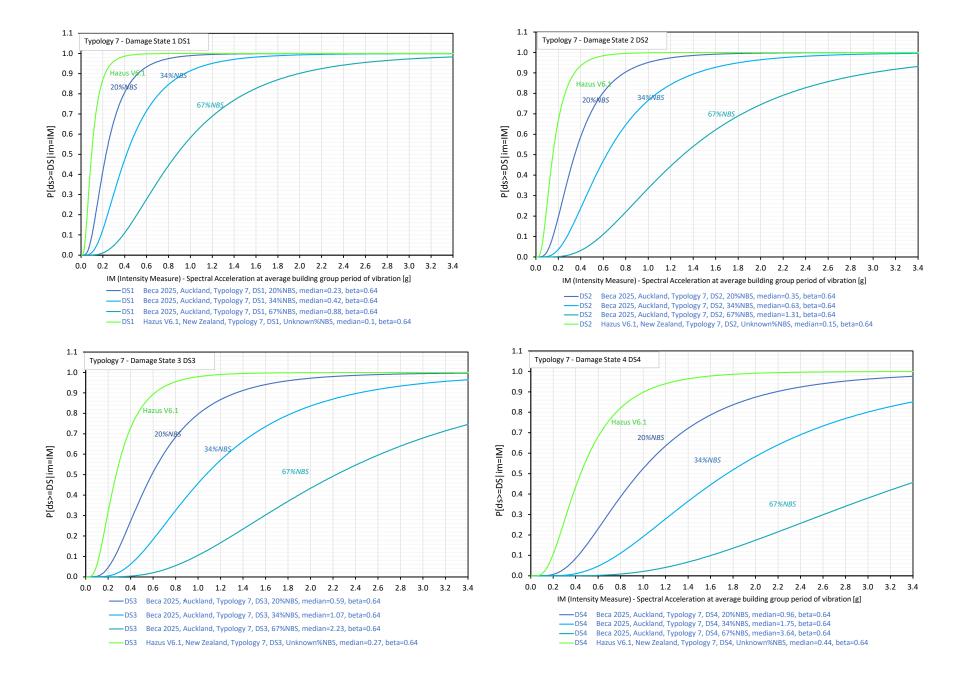
HAZUS v6.1 comparisons vs. DBM fragility curves

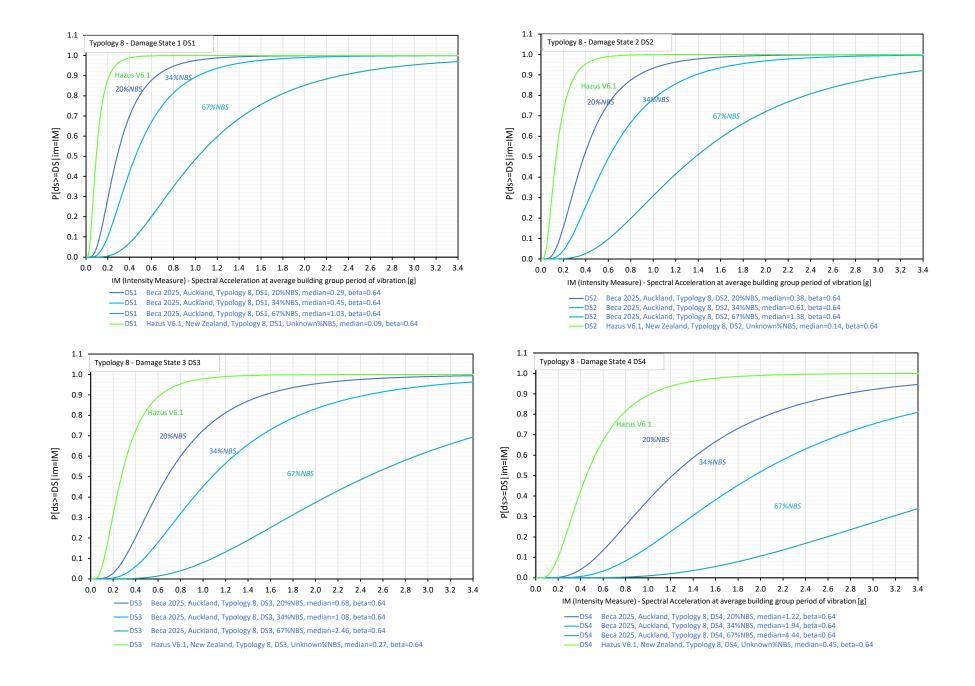


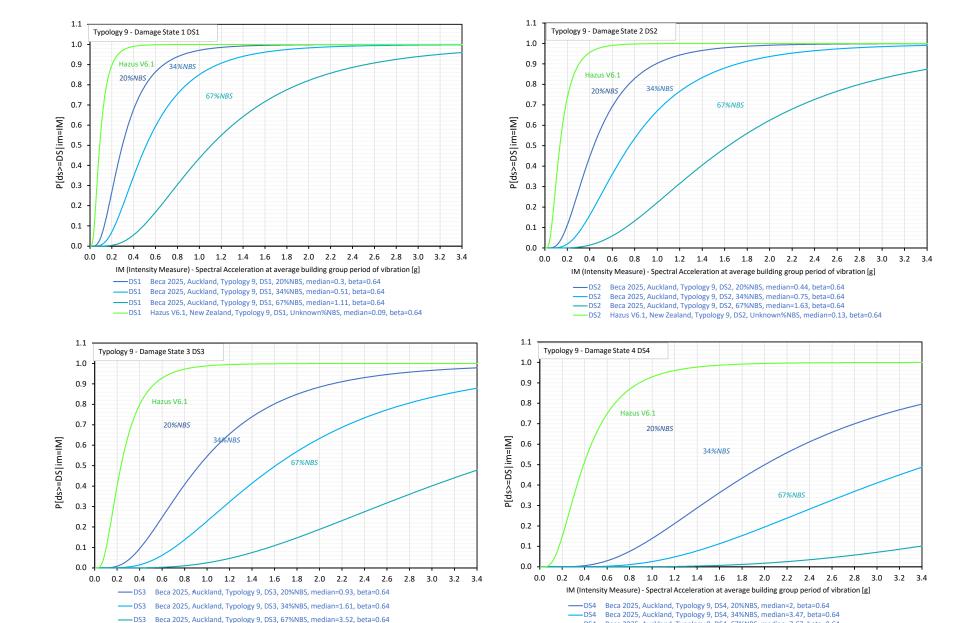








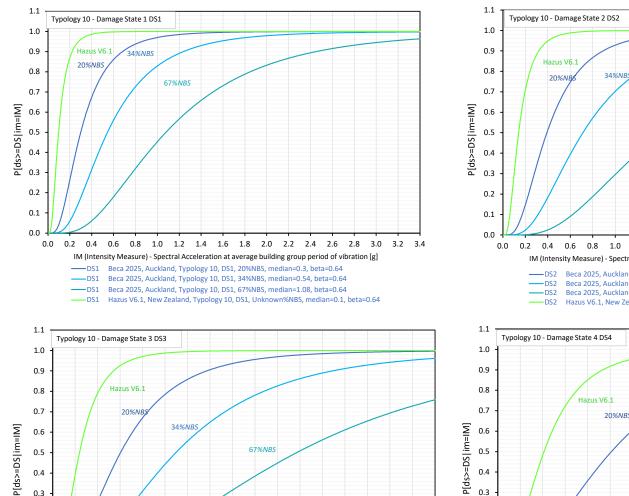




—— DS3 Hazus V6.1, New Zealand, Typology 9, DS3, Unknown%NBS, median=0.23, beta=0.64

— DS4 Beca 2025, Auckland, Typology 9, DS4, 67%NBS, median=7.67, beta=0.64

——DS4 Hazus V6.1, New Zealand, Typology 9, DS4, Unknown%NBS, median=0.39, beta=0.64



 $0.0 \quad 0.2 \quad 0.4 \quad 0.6 \quad 0.8 \quad 1.0 \quad 1.2 \quad 1.4 \quad 1.6 \quad 1.8 \quad 2.0 \quad 2.2 \quad 2.4 \quad 2.6 \quad 2.8 \quad 3.0 \quad 3.2 \quad 3.4$ 

——DS3 Beca 2025, Auckland, Typology 10, DS3, 20%NBS, median=0.6, beta=0.64

——DS3 Beca 2025, Auckland, Typology 10, DS3, 34%NBS, median=1.1, beta=0.64

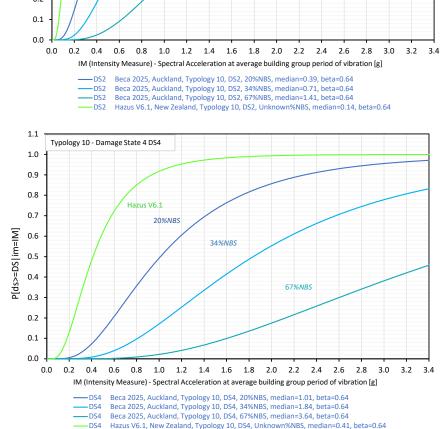
——DS3 Beca 2025, Auckland, Typology 10, DS3, 67%NBS, median=2.17, beta=0.64

—— DS3 Hazus V6.1, New Zealand, Typology 10, DS3, Unknown%NBS, median=0.24, beta=0.64

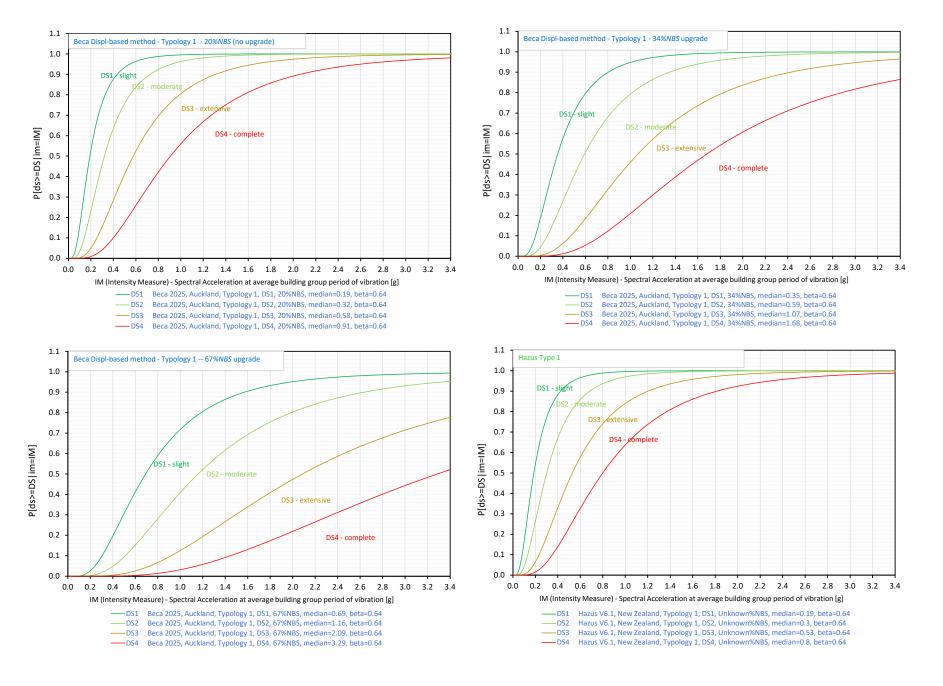
0.3

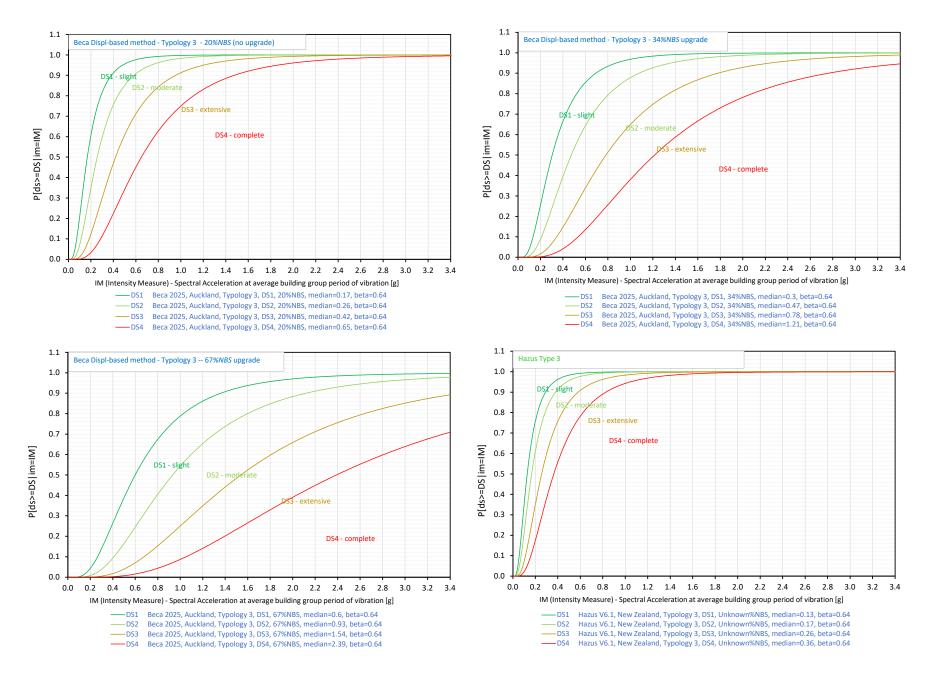
0.2

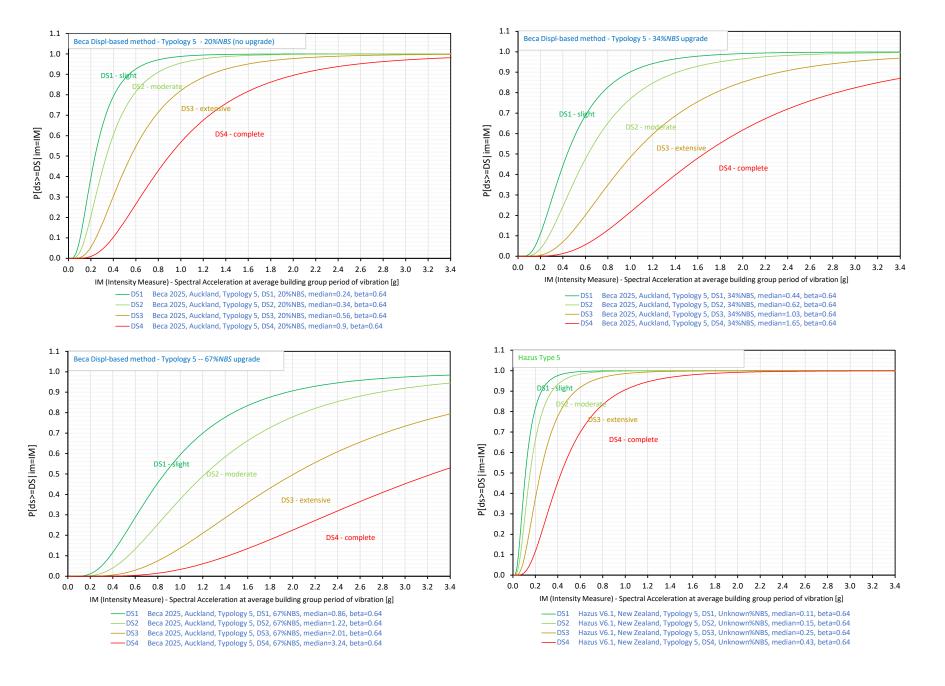
0.1

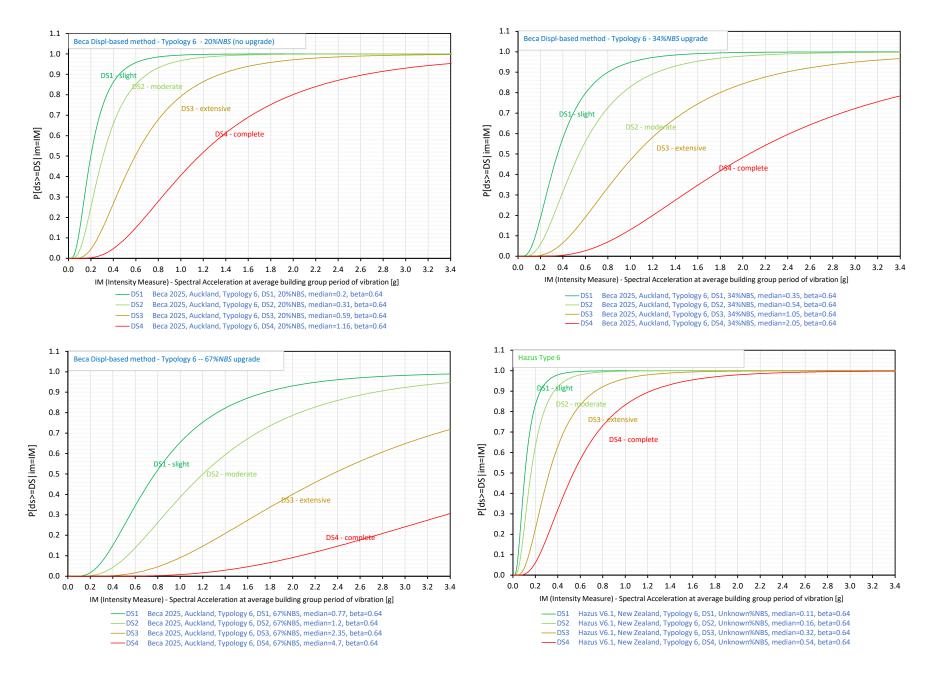


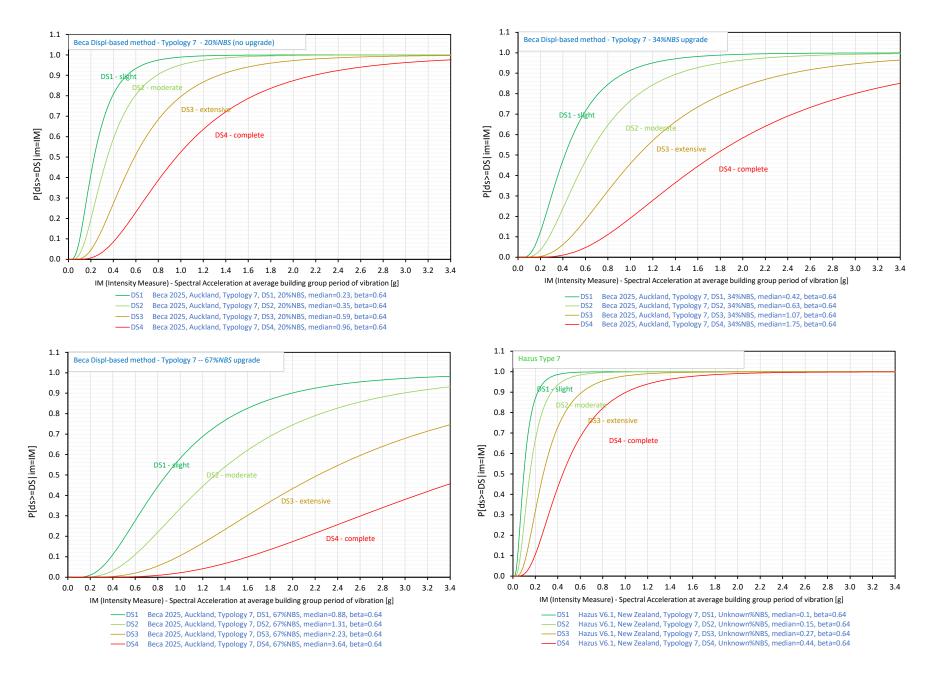
67%NBS

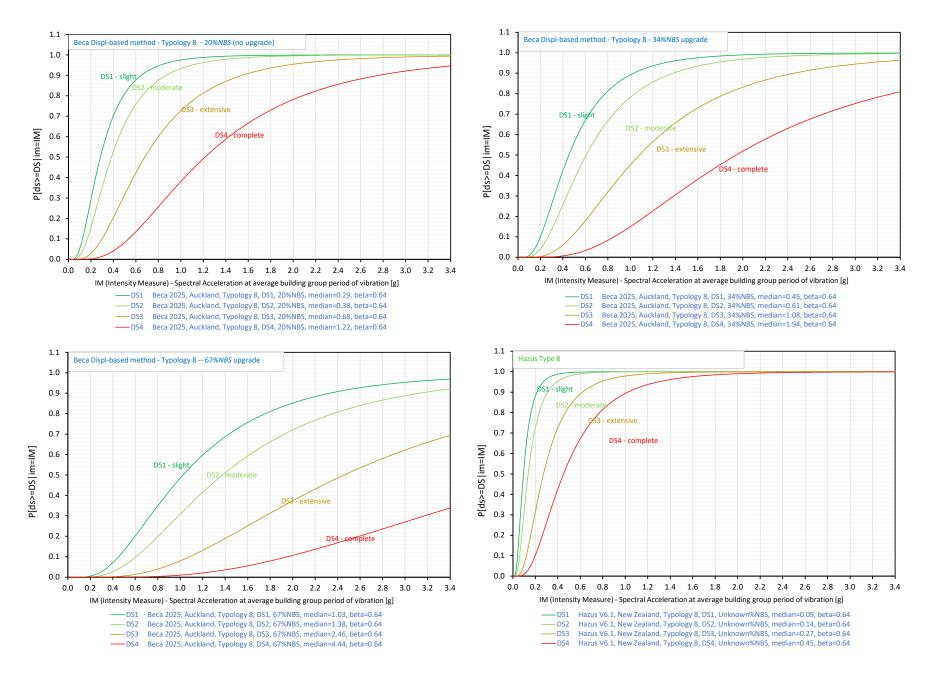


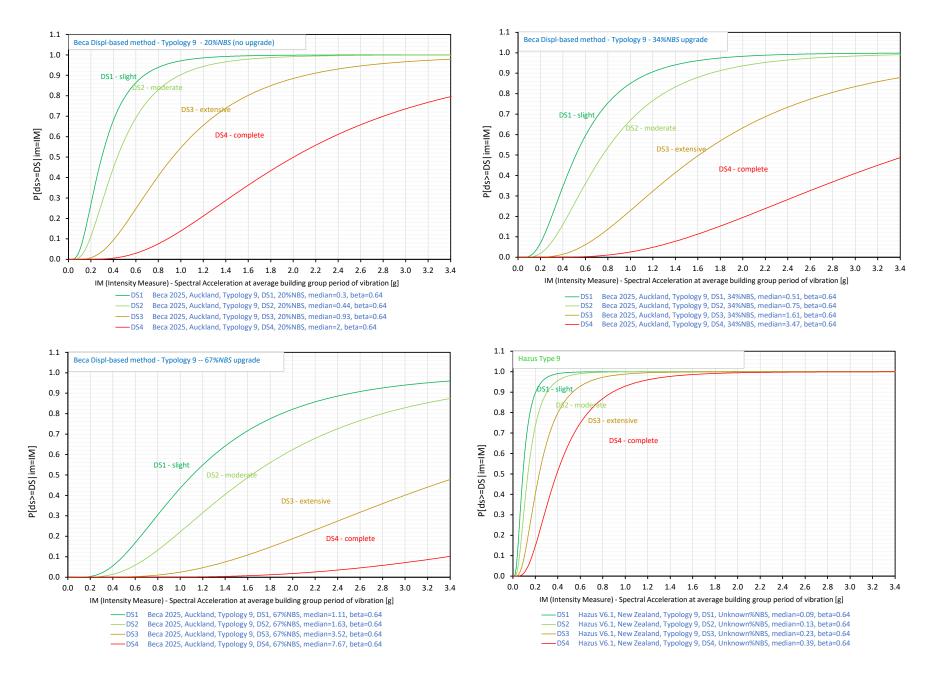


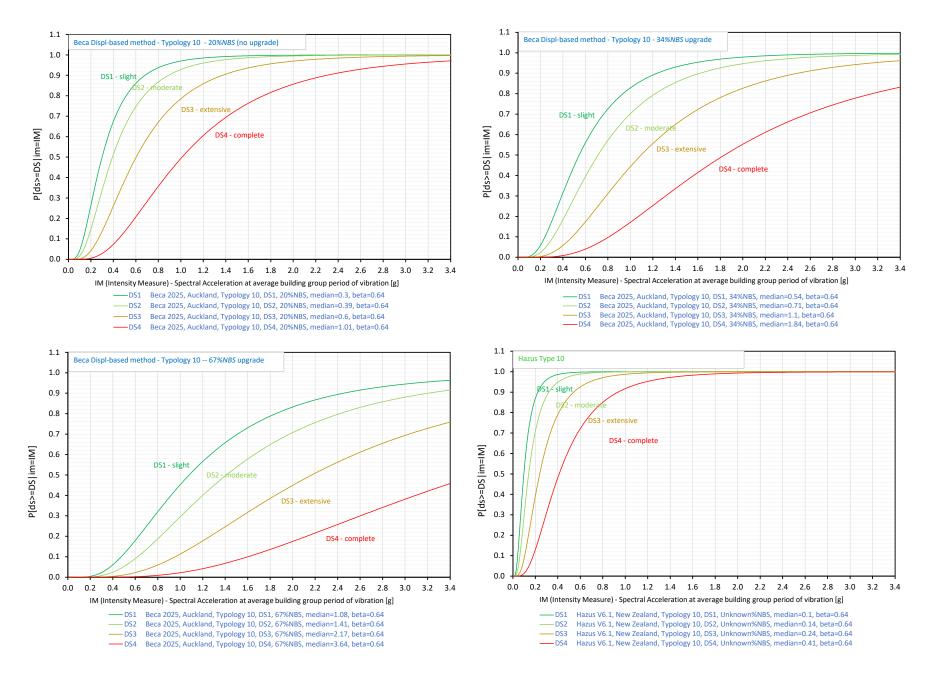














## Appendix G

# Past Earthquakes Comparison



## Appendix G – Past earthquakes – comparison

The following table was utilised as one of several high-level tools to assess the risk model and test input parameters versus loss estimates; however, this tool was not relied upon exclusively.

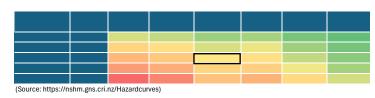
It is important to note that our study is not based on a specific scenario event and only focuses on earthquakeprone buildings within urban areas. Therefore, any direct comparison should be approached with caution. Additionally, in the Christchurch event, most fatalities were concentrated in just two buildings, whereas our study still overpredicts deaths compared to what occurred.

The Christchurch 2011 earthquake in New Zealand reported a death toll equivalent to 0.05% of the city's population. This is somewhat comparable to our study's findings for the "% death of city population – no upgrade" values, which are 0.02% in the "Low Model" and 0.04% in the "Mean Model" under Christchurch APoE (Annual Probability of Exceedance) 1:500 conditions.

Despite these limitations, this high-level comparison suggests that the final settings of our Low-Mean Model (30th percentile) are reasonably aligned with observed outcomes, though we acknowledge the inherent challenges in making direct comparisons.



## Hazard uniform Hazard Spectrum - spectral acceleration at 0.4 sec



assuming Vs30=275m/s, T1=0.4sec

**0.89g Christchurch Feb 2011,** average record of top 30 stations. Close match to APoE 1:500 Christchurch NSHM2022

## MEAN MODEL (50%til Consequence model)

APoE **	Location	SA(T1)	CS5 totals			EPB	total	CS5 % of EPB population			CS5 % of city population		
		[g]	no upgrade	34% <i>NBS</i>	67%NBS	population *	population	no upgrade	34%NBS	67%NBS	no upgrade	34%NBS	67%NBS
	Wellington	1.8			•	34,074	213,100	3%	2%	0.4%	0.5%	0.3%	0.06%
	Feilding	1.5	Ţ			4,578	17,550	2%	1%	0.2%	0.5%	0.2%	0.05%
1:500	Christchurch	0.95	I			36,949	389,300	2%	0%	0.1%	0.2%	0.0%	0.01%
	Whanganui	1.10	I			1,959	40,000	12%	4%	0.8%	0.6%	0.2%	0.04%
	Dunedin	0.59	I			14,378	130,400	5%	2%	0.3%	0.5%	0.2%	0.03%
	Auckland	0.31	Ţ			104,843	1,775,900	0%	0.1%	0.00%	0.0%	0.00%	0.000%
	Wellington	2.3	Ĭ			34,074	213,100	4%	3%	0.8%	0.7%	0.4%	0.12%
	Feilding	2	Ţ			4,578	17,550	2%	1%	0.3%	0.6%	0.3%	0.09%
1:1000	Christchurch	1.3	Ţ			36,949	389,300	2%	1%	0.1%	0.2%	0.1%	0.01%
	Whanganui	1.4	Ţ			1,959	40,000	14%	7%	1.6%	0.7%	0.3%	0.08%
	Dunedin	0.82	Ţ			14,378	130,400	6%	3%	0.7%	0.7%	0.3%	0.08%
	Auckland	0.44	Ţ			104,843	1,775,900	1%	0%	0.0%	0.1%	0.0%	0.001%
	Wellington	3.2	Ĭ			34,074	213,100	5%	4%	1.4%	0.8%	0.6%	0.23%
1:2500	Feilding	2.7	Ţ			4,578	17,550	3%	2%	0.7%	0.7%	0.5%	0.18%
1:2500	Christchurch	1.6	Ī			36,949	389,300	3%	1%	0.3%	0.3%	0.1%	0.03%
	Whanganui	1.9	Ţ			1,959	40,000	16%	10%	3.4%	0.8%	0.5%	0.17%
	Dunedin	1.2	Ī			14,378	130,400	8%	5%	1.6%	0.9%	0.5%	0.17%
	Auckland	0.67				104,843	1,775,900	2%	1%	0.1%	0.1%	0.0%	0.01%

Real Earthquakes	toll
Hawke's Bay, NZ 1931	1.60%
Long Beach, USA, 1933	0.05%
Mexico City, 1986	0.06%
Loma Prieta, USA, 1989	0.10%
Kobe, Japan, 1995	0.43%
Northridge , USA, 1994	0.05%
Haiti, 2010	5.14%
Tōhoku, Japan 2011	0.21%
Christchurch, NZ 2011	0.05%
Turkey & Syria, 2023	1.55%

Mean model appears conservative, high quanitties of CS5 when compared to real earthquake data

### LOW MODEL (10%til Consequence model)

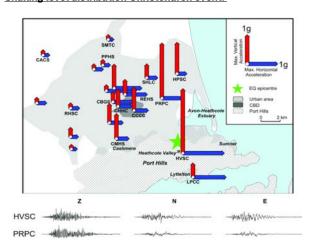
	Location	SA(T1)	CS5 totals		EPB total		CS5 % of EPB population			CS5 % of city population			
APoE **		[g]	no upgrade	34%NBS	67% <i>NBS</i>	population *	population	no upgrade	34%NBS	67%NBS	no upgrade	34%NBS	67%NBS
		1.8			-	34,074	213,100	1%	0%	0.2%	0.2%	0.0%	0.03%
		1.5				4,578	17,550	1%	0%	0.1%	0.2%	0.1%	0.02%
1:500		0.95				36,949	389,300	1%	0%	0.0%	0.1%	0.0%	0.00%
1.500		1.10				1,959	40,000	5%	2%	0.4%	0.3%	0.1%	0.02%
		0.59				14,378	130,400	2%	1%	0.1%	0.2%	0.1%	0.02%
		0.31				104,843	1,775,900	0%	0.0%	0.00%	0.0%	0.00%	0.0001%
		2.3				34,074	213,100	2%	1%	0.3%	0.3%	0.1%	0.05%
		2				4,578	17,550	1%	1%	0.2%	0.3%	0.1%	0.04%
1:1000		1.3				36,949	389,300	1%	0%	0.1%	0.1%	0.0%	0.01%
		1.4				1,959	40,000	6%	2%	0.8%	0.3%	0.1%	0.04%
		0.82				14,378	130,400	3%	1%	0.3%	0.3%	0.1%	0.03%
		0.44				104,843	1,775,900	0%	0%	0.0%	0.0%	0.0%	0.000%
		3.2				34,074	213,100	2%	1%	0.6%	0.3%	0.2%	0.10%
1:2500		2.7				4,578	17,550	1%	1%	0.3%	0.3%	0.2%	0.07%
1.2500		1.6				36,949	389,300	1%	1%	0.1%	0.1%	0.1%	0.01%
		1.9				1,959	40,000	7%	5%	1.5%	0.4%	0.2%	0.08%
		1.2				14,378	130,400	4%	2%	0.7%	0.4%	0.2%	0.08%
		0.67				104,843	1,775,900	1%	0%	0.0%	0.1%	0.0%	0.00%

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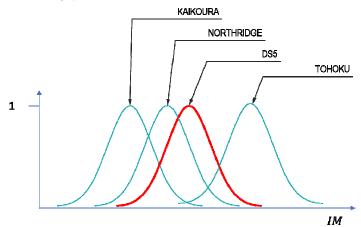
Lower model CS5 quantities closer to real earthquake data

Earthquake	Year	<b>Dsathtal</b> d	Population (estimate only)	Magnitude	Distance	Depth	% of population
Haiyuan, China	1920	180,000	3,000,000	M 8.3	~10km from Haiyuan County	~15km	6%
Kanto, Japan	1923	143,000	4,500,000	M 7.9	Epicenter near the Sagami Bay (~80km from Tokyo)	~23km	3%
Nanchang, China (1927)	1927	200,000	3,000,000	M 7.6	M 7.6 No info		7%
Ashgabat, Turkmenistan	1948	110,000	1,000,000	M 7.3	M 7.3 Near Ashgabat (~10km)		11%
Tangshan, China	1976	242,000–650,000	2,000,000	M 7.5	M 7.5 Directly under Tangshan (~0 km)		10%
Sumatra, Indonesia	2004	227,898	2,600,000	M 9.1	Offshore (~250km from Banda Aceh)	~30km	8.8%
Haiti	2010	100,000–316,000	2,100,000	M 7.0	Epicenter near Léogâne (~25km from Port-au-Prince)	~13km	5.1%
Sumatra, Indonesia Haiti Sichuan, China Muzaffarabad, Pakistan Mexico City Kobe Earthquake, Japan Tõhoku Earthquake and Tsunami	2008	87,587	11,000,000	M 7.9	Epicenter in Wenchuan County (~80km from Chengdu)	~19km	0.8%
Muzaffarabad, Pakistan	2005	73,338	650,000	M 7.6	Not well-documented		11%
Mexico City	1985	10,000	18,000,000	M8.1	Michoacán (~350km from Mexico City)	~15km	0.06%
Kobe Earthquake, Japan	1995	6,434	1,500,000	M6.9	~20km from Kobe	~16km	0.43%
Tōhoku Earthquake and Tsunami	2011	18,500	9,000,000	M9.0	(~70km east of Sendai)	~29km	0.21%
Long Beach Earthquake, USA	1933	120	250,000	M6.4	Newport-Inglewood Fault Line near Long Beach		0.05%
Loma Prieta Earthquake	1989	63 deaths, 3,757 injuries	62,956 Santa Cruz		peak accelration 0.65 g (at epicenter), MMI IX		0.10%
Northridge Earthquake, USA	1994	57	9,000,000	M 6.7	~30km northwest of downtown Los Angeles	~18km	0.001%
Puebla-Morelos, Mexico	2017	370	18,000,000	M7.1	~120km from Mexico City	~51km	0.00%
Turkey & Syria	2023	62,013	4,000,000	M 7.8			1.55%
Napier-Hawke's Bay, New Zealand	1931	256	16,000	M 7.8			1.60%
Christchurch, New Zealand	Feb-11	185	376,700	M 6.3	~10km from Christchurch	~5km	0.05%
Christchurch, New Zealand	Sep-10	0	376,700	M7.1	~40km west of Christchurch	10km	0%
Christchurch, New Zealand Christchurch, New Zealand Kaikōura Earthquake	2016	2 deaths and 618 injuries	212,000 (Wellington) 2,080 (Kaikoura)	M 7.8	~60km from Kaikōura, ~300km from Wellington	15km	0.001%

## **Shaking level distribution Christchurch event:**



Create a distribution of intensity measures for each earthquake and relate them to current fragility distribution



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